
Axions and their Relatives: Theory and Experiment

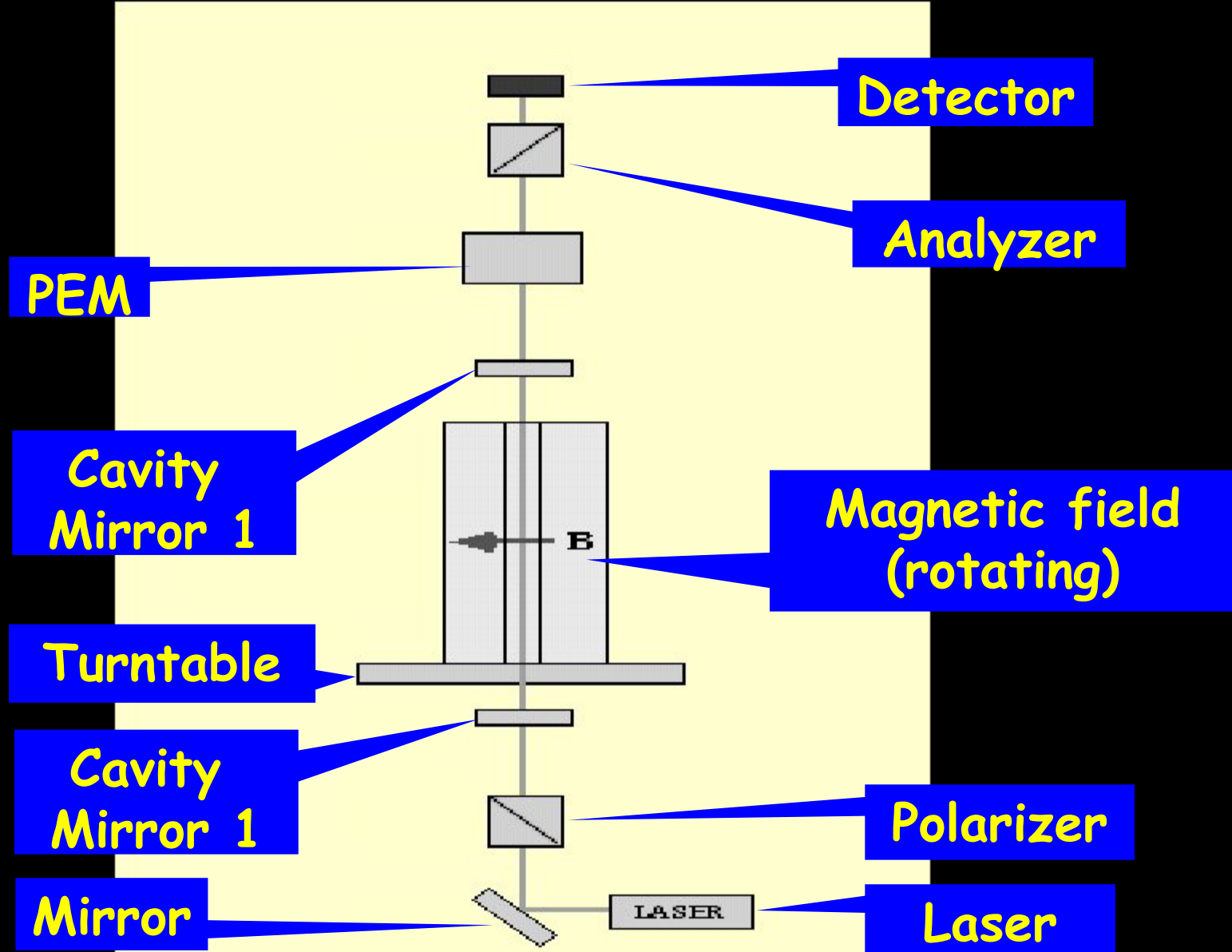


Joerg Jaeckel
DESY

PVLAS:

An unexpected Result

The Experiment

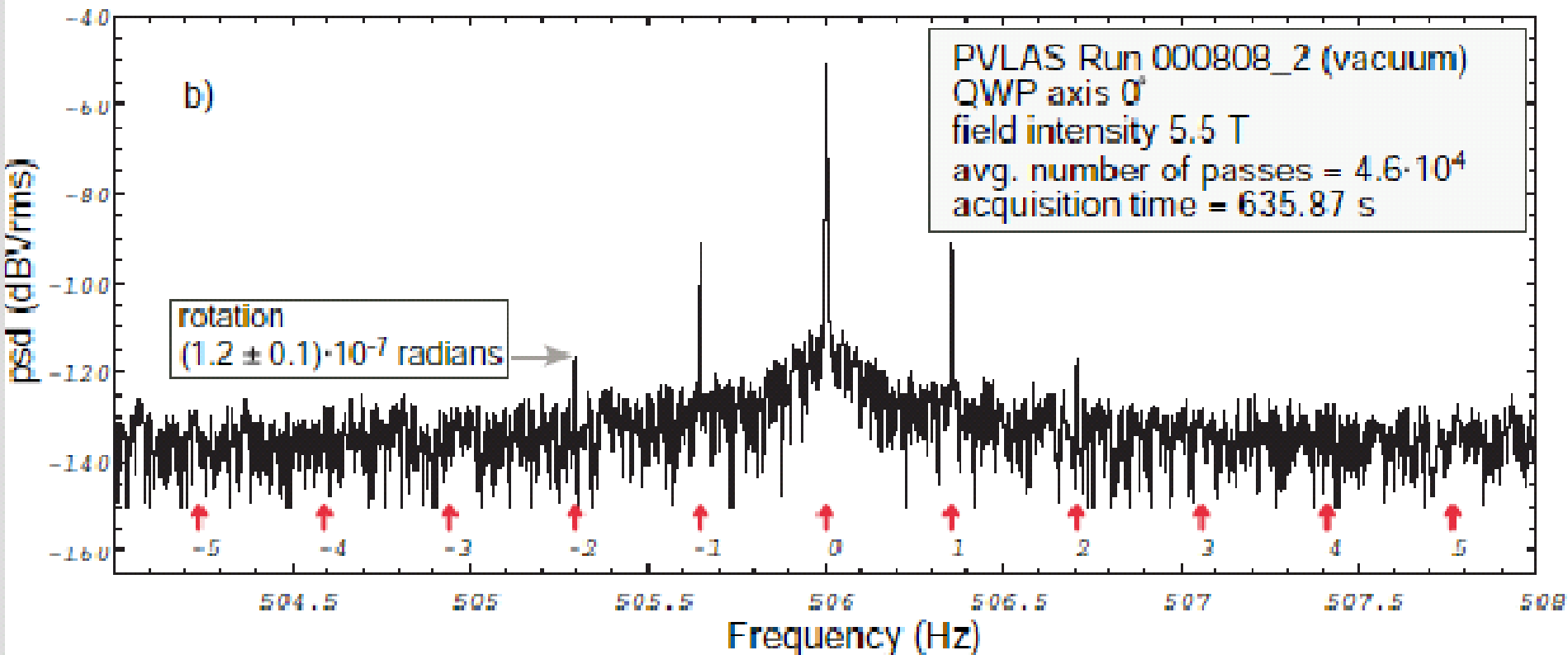


Goal



- Measure the **change in polarization** when light passes through **B-field**:
 - Rotation of the polarization
 - Ellipticity (phase shift),
i.e., linear polarized light is changed into (partly) circular polarized light.
-

Result (rotation)

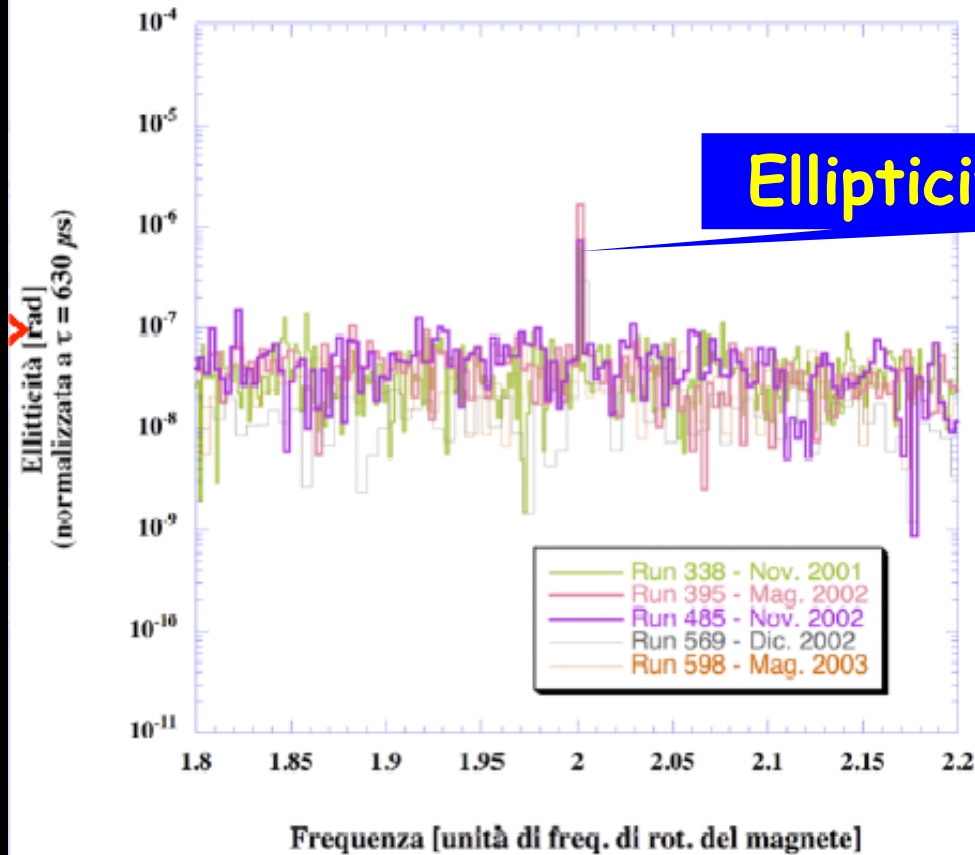


$$\frac{\text{rotation}}{\text{pass}} = \frac{\epsilon}{N} \sim 2.6 \cdot 10^{-12} \text{ rad}$$

Result (ellipticity)



Dati in vuoto con $B = 5.5 \text{ T}$
Ellitticità normalizzata a $\tau = 630 \mu\text{s}$



$B = 5.5 \text{ T}$
 $N \approx 97000$

Ellipticity $\approx 6 \cdot 10^{-7} \text{ rad}$

$$\frac{\text{ellipticity}}{\text{pass}} = \frac{\psi}{N} \sim 6 \cdot 10^{-12} \text{ rad}$$

A possible Interpretation



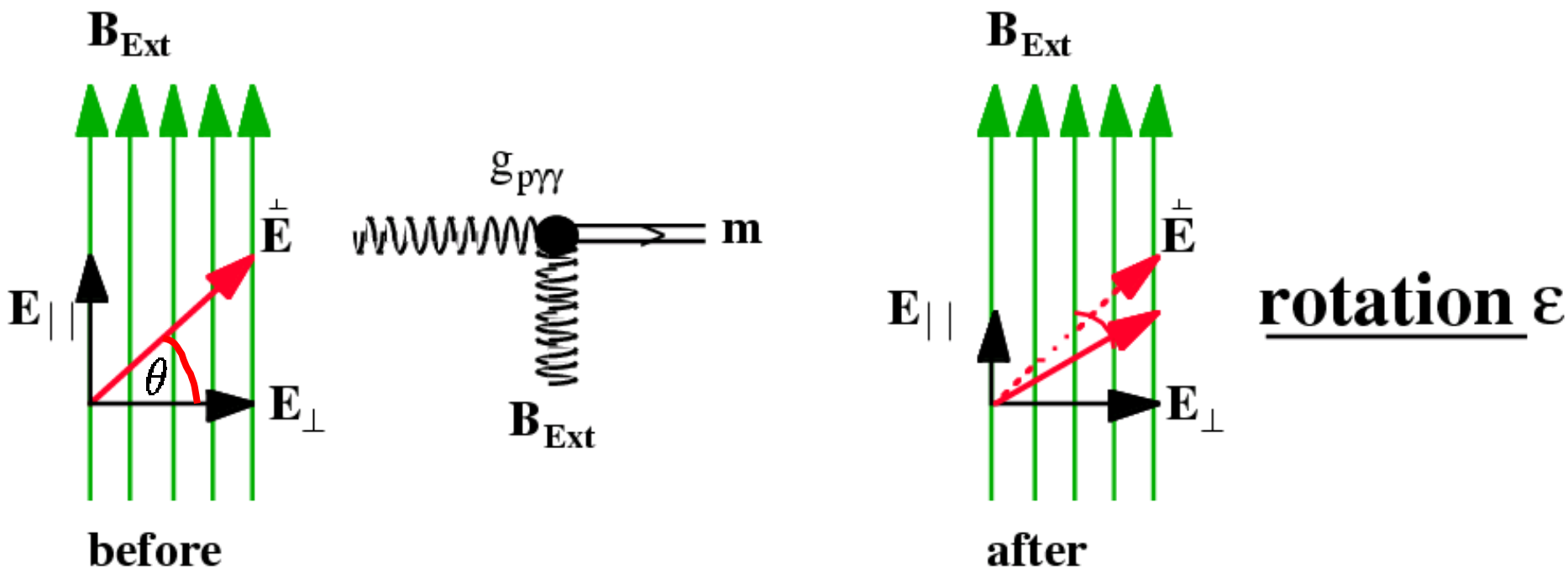
- Photons are converted into light (pseudo-)scalars



Dichroism (Rotation)



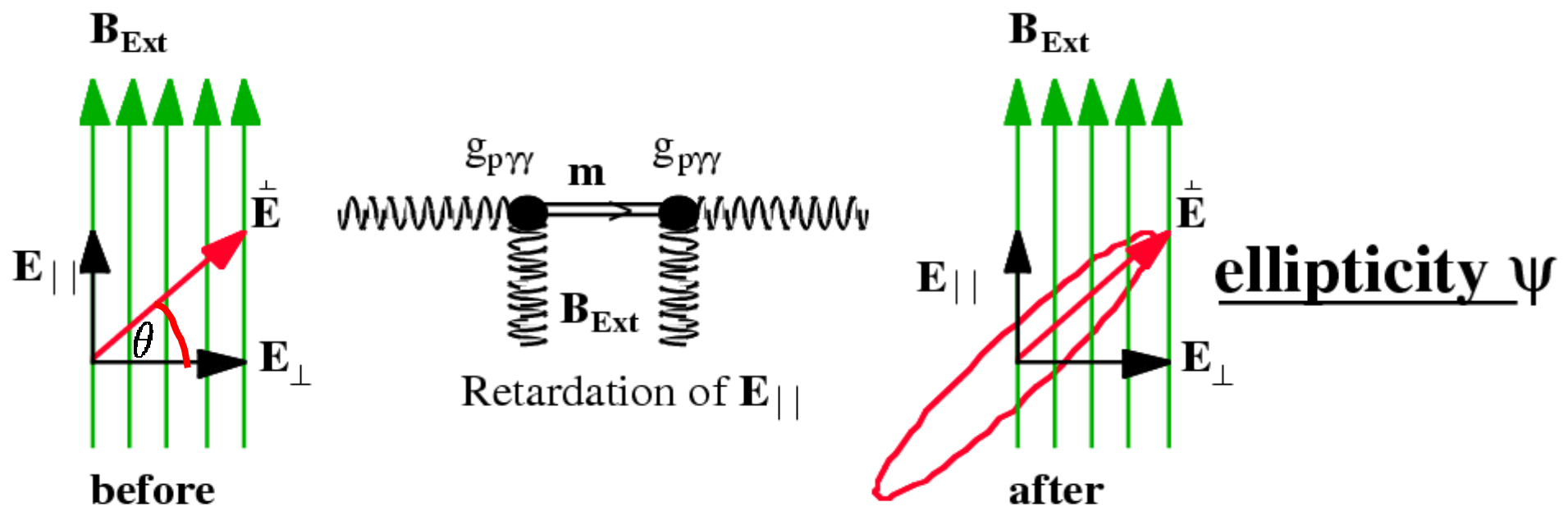
- Coupling $\mathcal{L} \sim g a F^{\mu\nu} \tilde{F}_{\mu\nu} \sim g a \vec{E} \cdot \vec{B}$



$$\epsilon \approx -N \left(\frac{gBL}{4} \right)^2 \sin(2\theta)$$

Ellipticity

Virtual ALP production leads to Birefringence





$$\psi \approx \frac{N}{6} \left(\frac{gBL}{4} \right)^2 \frac{m_a^2 L}{\omega} \sin(2\theta)$$

A possible Interpretation



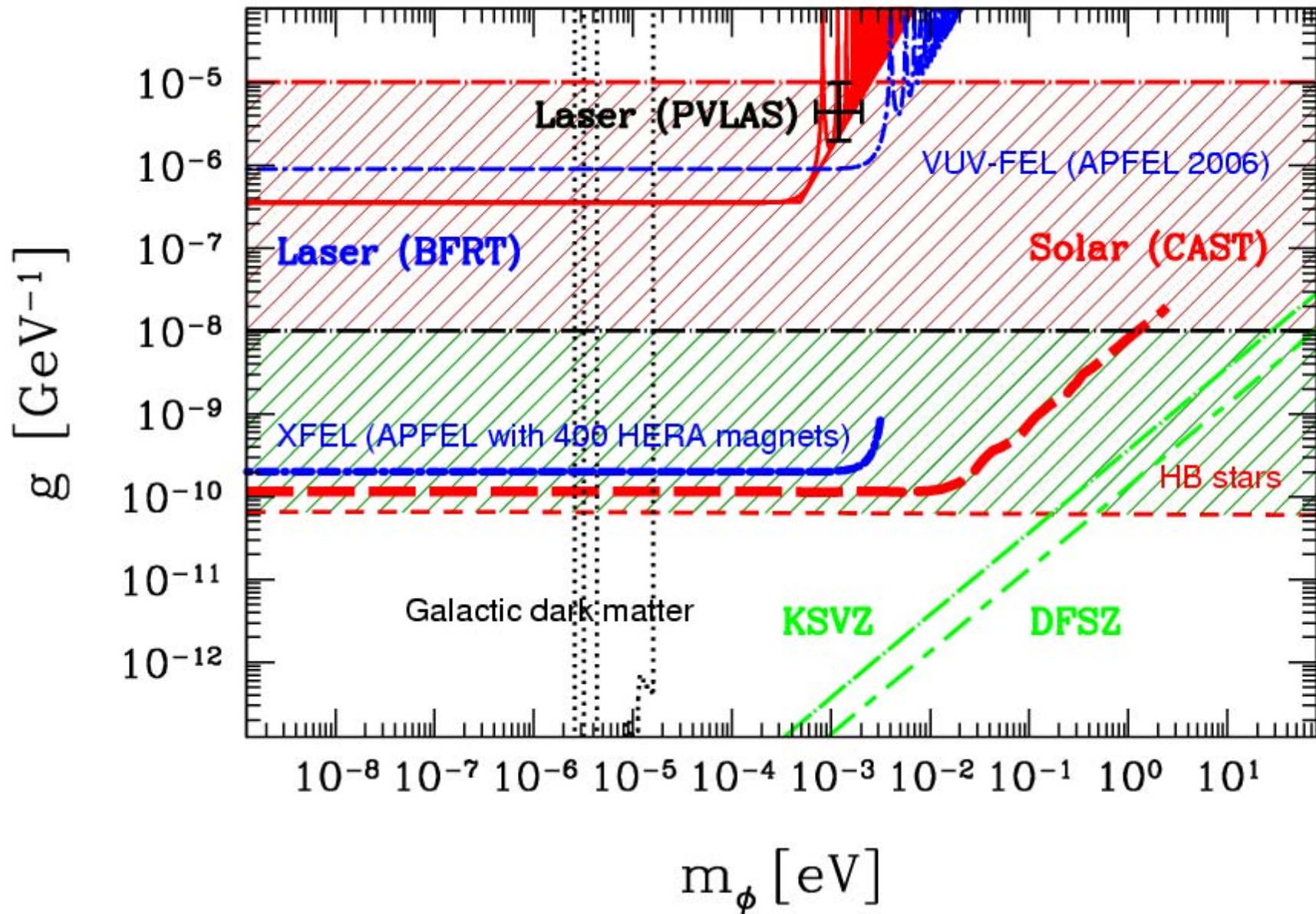
- Photons are converted into light (pseudo-)scalars
 - With mass $m = (1 - 1.5) \text{ meV}$
 $g = (1.7 - 5) \times 10^{-6} \text{ GeV}^{-1}$
-

0. Overview



- 1. Axions and their Relatives
 - 2. Astrophysical Bounds
 - 3. PVLAS again
 - 4. Evading Astrophysical Bounds
 - 5. The future: Light shining through walls
 - 6. Conclusions
-

Overview Picture



1. Axioms and their Relatives

The QCD Action



$$S = \int d^4x \left[-\frac{1}{4} F^{\mu\nu} F_{\mu\nu} - \frac{\theta}{4} F^{\mu\nu} \tilde{F}_{\mu\nu} + \bar{\psi} D_{\mu} \gamma^{\mu} \psi + \bar{\psi} M \psi \right]$$

- The θ -term is a total divergence!
- That does not mean it can be neglected!

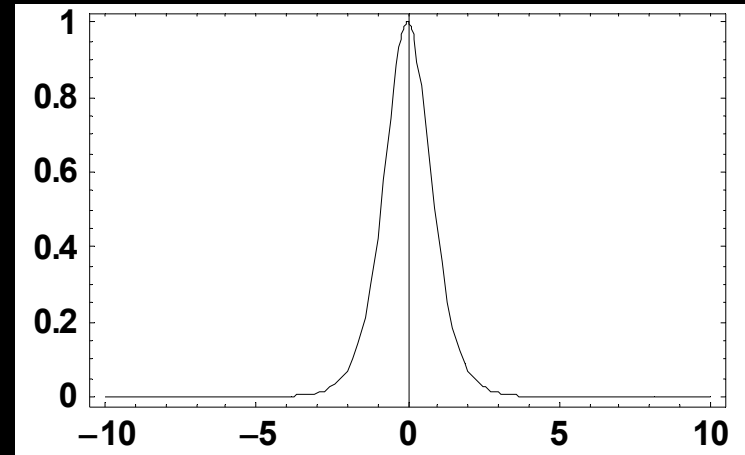
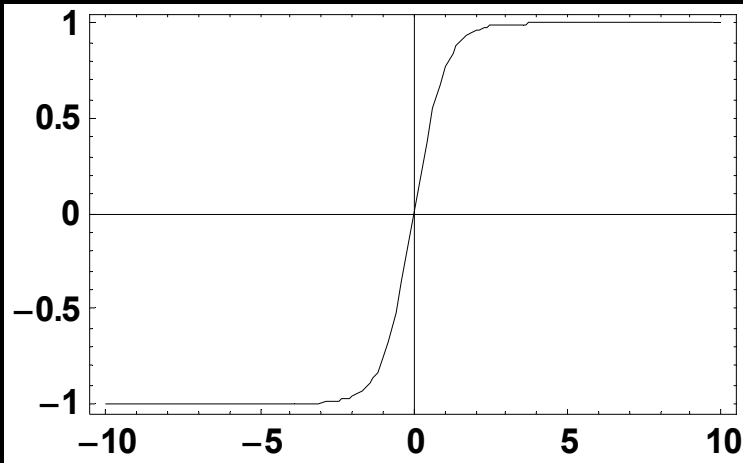
 θ has observable consequences!

Boundaries matter! - An analogy

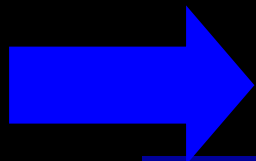


$$\tanh(x)$$

$$\frac{d}{dx} \tanh(x)$$



$$\int_{-\infty}^{\infty} dx \frac{d}{dx} \tanh(x) = 2 \neq 0$$



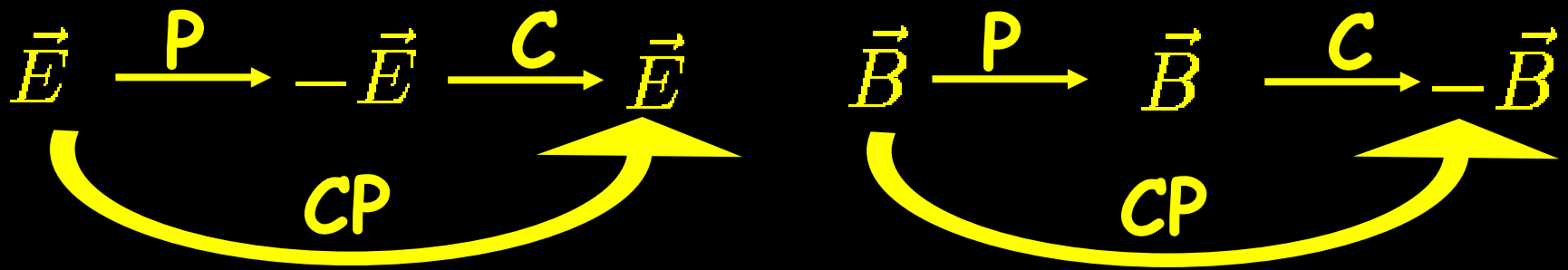
**Boundary terms can
not always be neglected!**

It's CP violating



- The θ -term violates CP:

$$F_{\mu\nu} \tilde{F}^{\mu\nu} \sim \vec{E} \cdot \vec{B}$$



A large red arrow points from the left towards the equation below.

$$\vec{E} \cdot \vec{B} \xrightarrow{CP} -\vec{E} \cdot \vec{B}$$

θ can be measured



- θ -term is a color singlet!

 Search for CP violation in hadrons!

- Electric dipole moment is CP violating!

$$H \sim \vec{d} \cdot \vec{E} \sim q\vec{S} \cdot \vec{E}$$

 Measure EDM of the neutron!

One finds...nothing



• Calculation: $|\vec{d}| \sim 1 - 10 \times 10^{-16} e cm \theta$

• Measurement: $|\vec{d}| < 3 \cdot 10^{-26} e cm$

➔ $|\theta| < 3 \cdot 10^{-10}$

➔ Extremely unnatural!

➔ Strong CP Problem!

The Axion Solution

A Dynamical θ



- **Idea:**

- Make θ a dynamical degree of freedom a
- Let a have no tree level potential
- Let a have only derivative couplings

- **Then:**

$$\begin{aligned} \exp\left(-\int_x V(a)\right) &= \left| \int \mathcal{D}A_\mu \exp(-S_{eff}[\phi, A^\mu]) \exp\left(-i\frac{a}{32\pi^2} \int_x F^{\mu\nu} \tilde{F}_{\mu\nu}\right) \right| \\ &\leq \int \mathcal{D}A_\mu \left| \exp(-S_{eff}[\phi, A^\mu]) \exp\left(-i\frac{a}{32\pi^2} \int_x F^{\mu\nu} \tilde{F}_{\mu\nu}\right) \right| \\ &\leq \int \mathcal{D}A_\mu \exp(-S_{eff}[\phi, A^\mu]) \\ &\leq \exp\left(-\int_x V[0]\right) \end{aligned}$$

A Dynamical θ



- **Idea:**

- Make θ a dynamical degree of freedom.
- Let θ have no tree level potential
- Let θ have only derivative couplings

- **Then:**

→ $V[0] \leq V[a] \quad \forall a$

→ a will evolve to $a=\theta=0$

→ CP is conserved

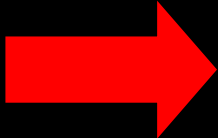
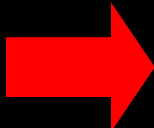
What is a?



- Properties:

- Let a be a dynamical degree of freedom.
- Let a have no tree level potential
- Let a have only derivative couplings

- $a \in [0, 2\pi]$ since $\int d^4x \frac{F_{\mu\nu} \tilde{F}^{\mu\nu}}{32\pi^2} = n \in \mathbb{Z}$

 a is Goldstone boson
of a $U(1)$ symmetry  Axion!

Peccei-Quinn Symmetry



- Toy model:

$$\mathcal{L} = -\frac{1}{4}F^2 + i\bar{\psi}D_\mu\gamma^\mu\psi - |\partial_\mu\phi|^2 - \mu^2|\phi|^2 - \lambda|\phi|^4 + \bar{\psi}\left(G\phi\frac{1+\gamma_5}{2} + G^*\phi^*\frac{1-\gamma_5}{2}\right)\psi$$

- U(1):
 $\phi \rightarrow \exp(i\alpha)\phi$
 $\psi \rightarrow \exp\left(-i\frac{\alpha}{2}\gamma_5\right)\psi$

- If $\mu^2 < 0$ we have SSB

➡ Phase is Goldstone ➡ Use it as Axion

The Coupling to $F \tilde{F}$



- Adler-Bell-Jackiw anomaly

$$\partial_\mu j^\mu = \frac{g^2}{16\pi^2} F^{\mu\nu} \tilde{F}_{\mu\nu}$$

- Chiral rotations not a good symmetry:
it is anomalous

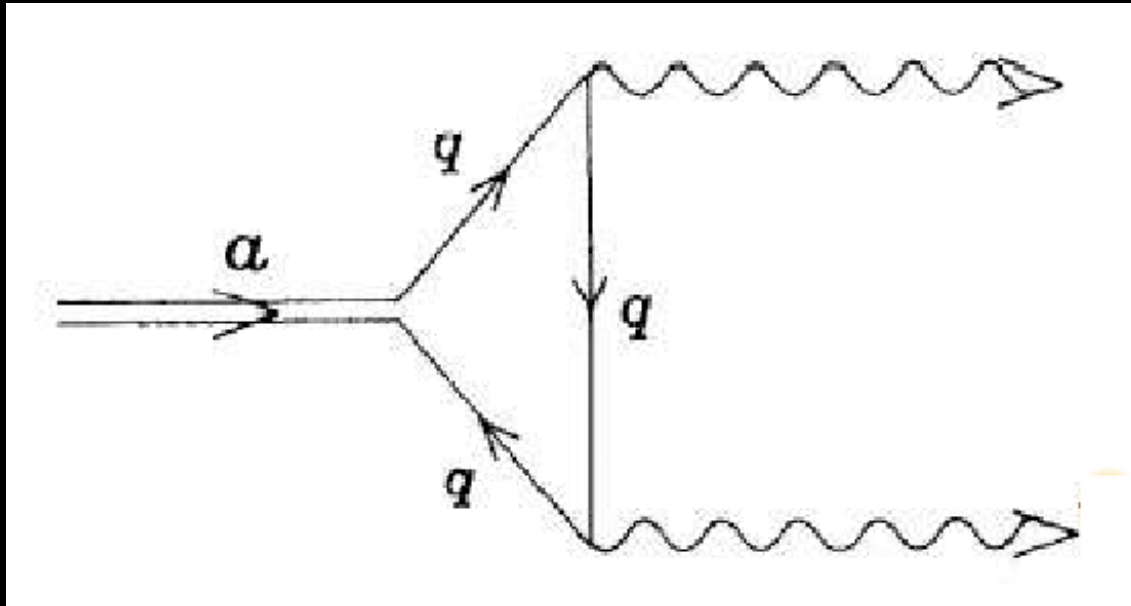
$$d\mu' = \mathcal{D}\psi' \mathcal{D}\bar{\psi}' = d\mu \exp \left(-1 \int_x \frac{\alpha}{2} \frac{1}{8\pi^2} \text{Tr} F^{\mu\nu} \tilde{F}_{\mu\nu} \right)$$

$$\psi' = \exp \left(-i \frac{\alpha}{2} \gamma_5 \right) \psi$$

The Coupling to $F \tilde{F}$



- A diagram



The mass of the Axion



- $U(1)_{PQ}$ is not exact

➡ Goldstone ➡ Pseudogoldstone

- Dimensional considerations

- SSB scale

$$\sim f_X$$

- Coupling to $F \tilde{F}$:

$$\sim \frac{a}{f_X} F^{\mu\nu} \tilde{F}_{\mu\nu}$$

- Scale of explicit breaking

$$\frac{1}{f_X} \langle F^{\mu\nu} \tilde{F}_{\mu\nu} \rangle \sim \frac{\Lambda^4}{f_X}$$

➡ Goldstone mass $m_a^2 \sim \frac{\Lambda^4}{f_X^2}$

The Coupling to $F_{em} \tilde{F}_{em}$

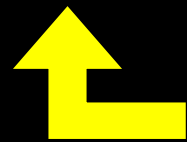


- Analog to F_{strong} coupling (anomaly)
- Differs by a factor of roughly α
- More precisely, with

$$\mathcal{L}_F = g\alpha F^{\mu\nu} \tilde{F}_{\mu\nu}$$

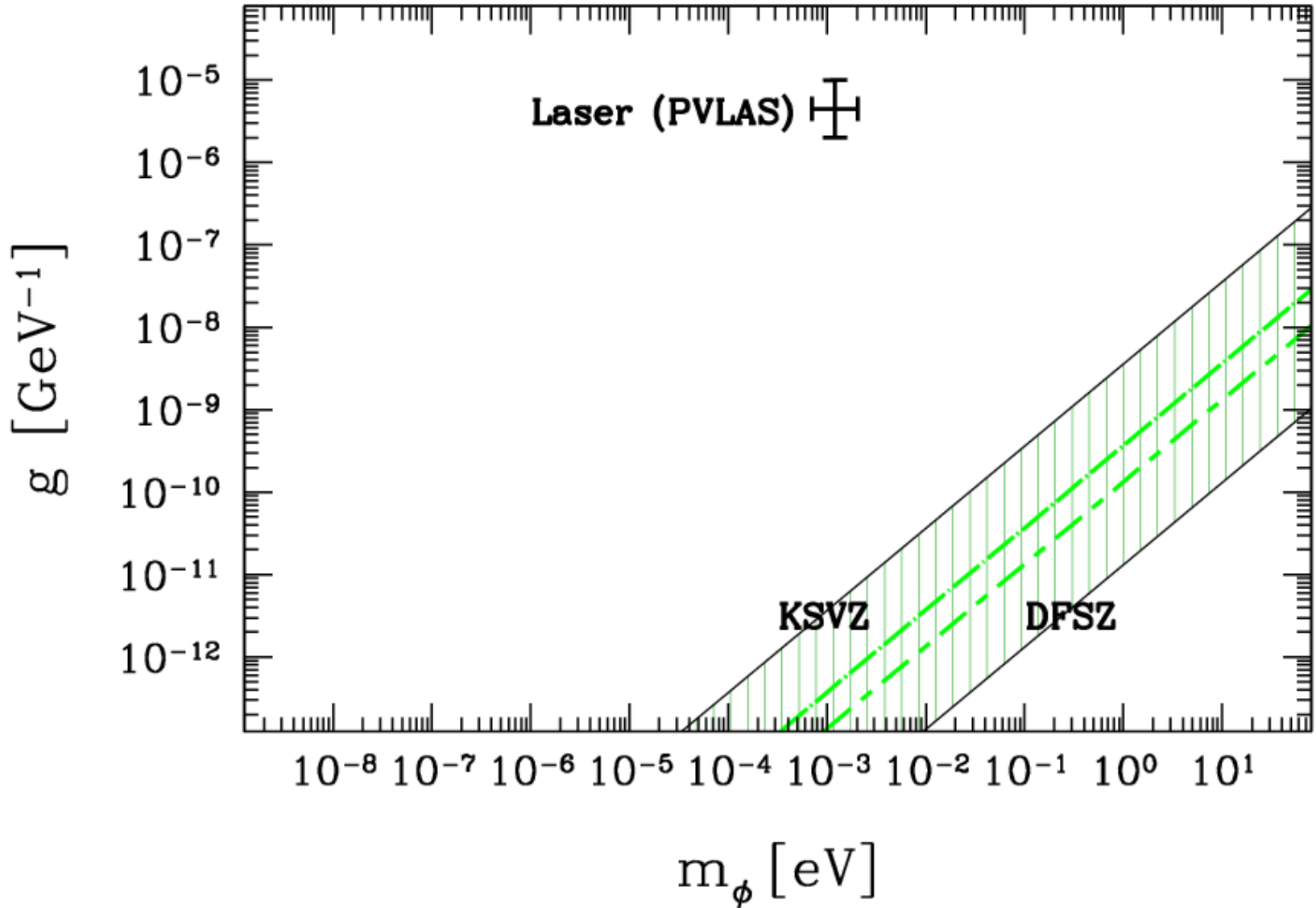
- Relation between M and m_a :

$$m_a g^{-1} = \mathcal{O}(1) \frac{\pi}{\alpha} m_\pi f_\pi \frac{\sqrt{m_u m_d}}{m_u + m_d}$$



(model dependent)

The Coupling to $F_{em} \tilde{F}_{em}$



The Relatives: ALPs



- Pseudoscalars: not very creative...
...Simply throw away m-g-relation
 - Scalars: as above but with coupling to F_{em}^2 instead of $F_{em}\tilde{F}_{em}$
-

Commercials

Your CP is violated to strongly?

An electric dipole moment is
generated by messy θ -term
effects?

Use Axion!

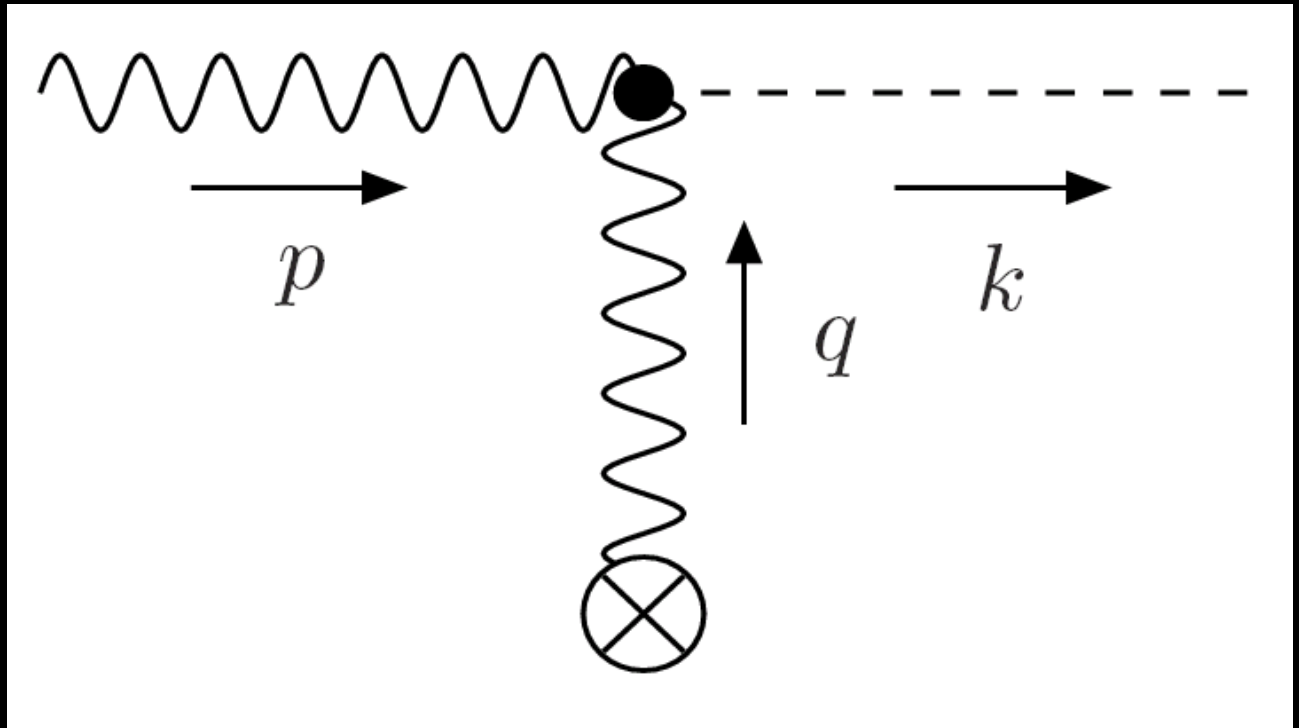


**New! With special cleaning particles
and extra strong photon coupling.**

2. Astrophysical Bounds

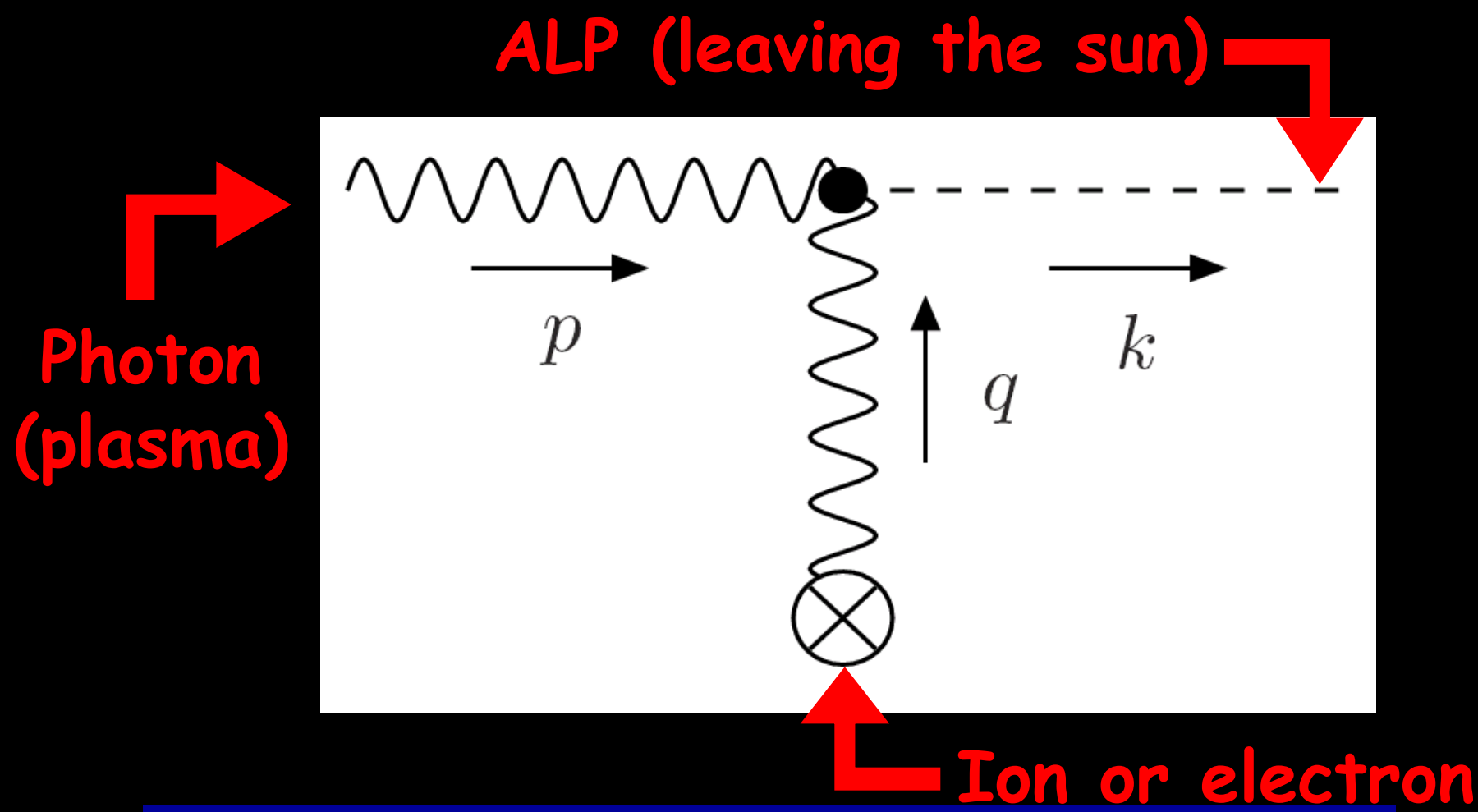
Tests are based on $F_{em} \tilde{F}_{em}$ coupling

- Primakoff proces



Tests are based on $F_{em} \tilde{F}_{em}$ coupling

- Primakoff process (in the sun)



We would freeze...



- If the coupling g is too large the sun would have died long ago.

- Why?

Axions can leave the sun without further interaction (in contrast to photons)

➡ Large energy loss from axion emission

➡ Sun burns fuel faster

➡ Sun would have died long ago

A (Very) Moderate Bound




- Without ALPs sun has fuel for about 10^{10} years

- Energy loss via Alps: $L_a \approx 1.7 \cdot 10^9 (g \cdot 10^4 \text{ GeV})^2 L_\gamma$

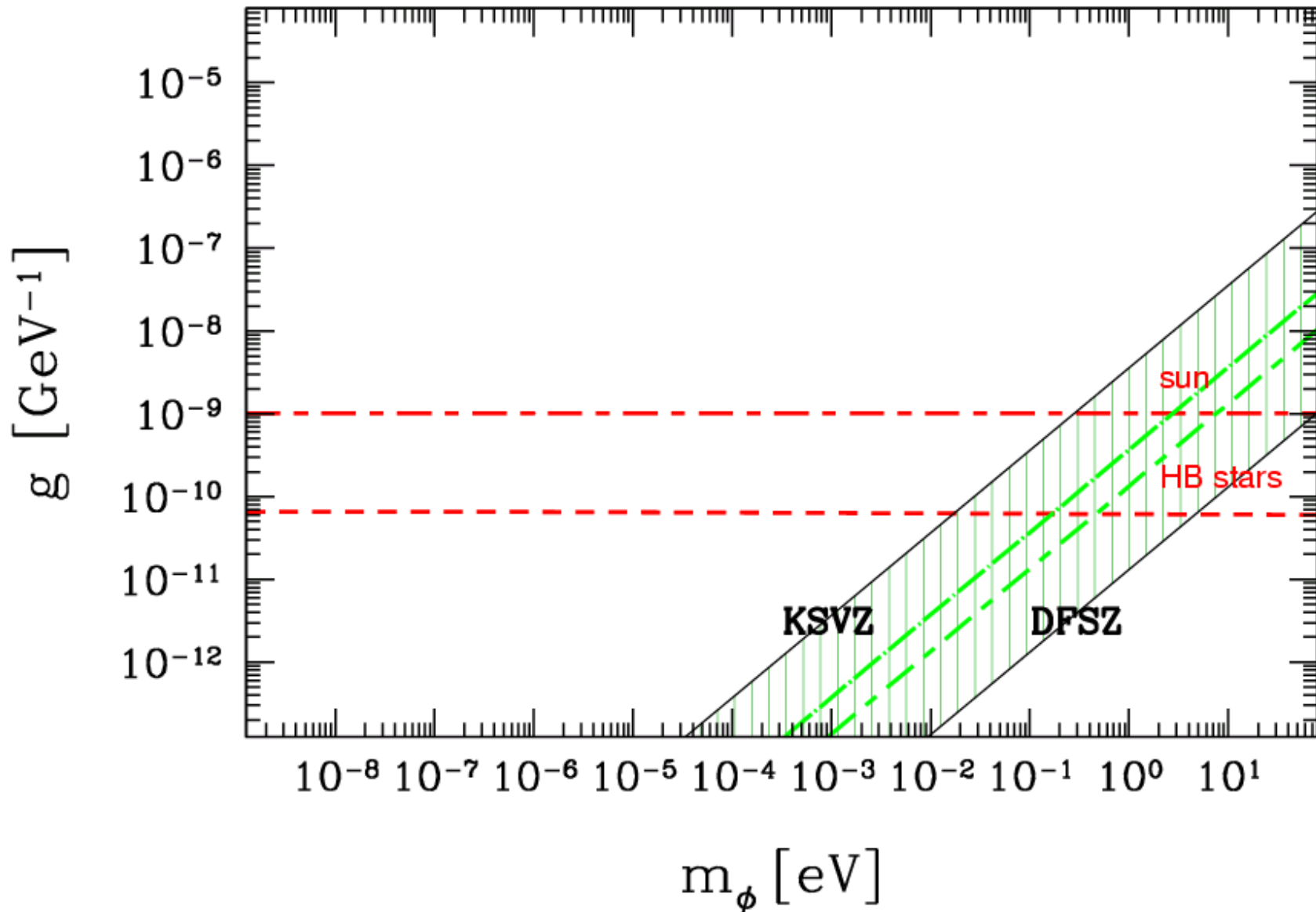
- Sun Lifetime with ALPs

$$t_{sun} \sim \frac{10 \text{ years}}{(g \cdot 10^4 \text{ GeV})^2}$$

- Pretty sure sun has been around for more than 10 years

 $g \leq 10^{-4} \text{ GeV}^{-1}$

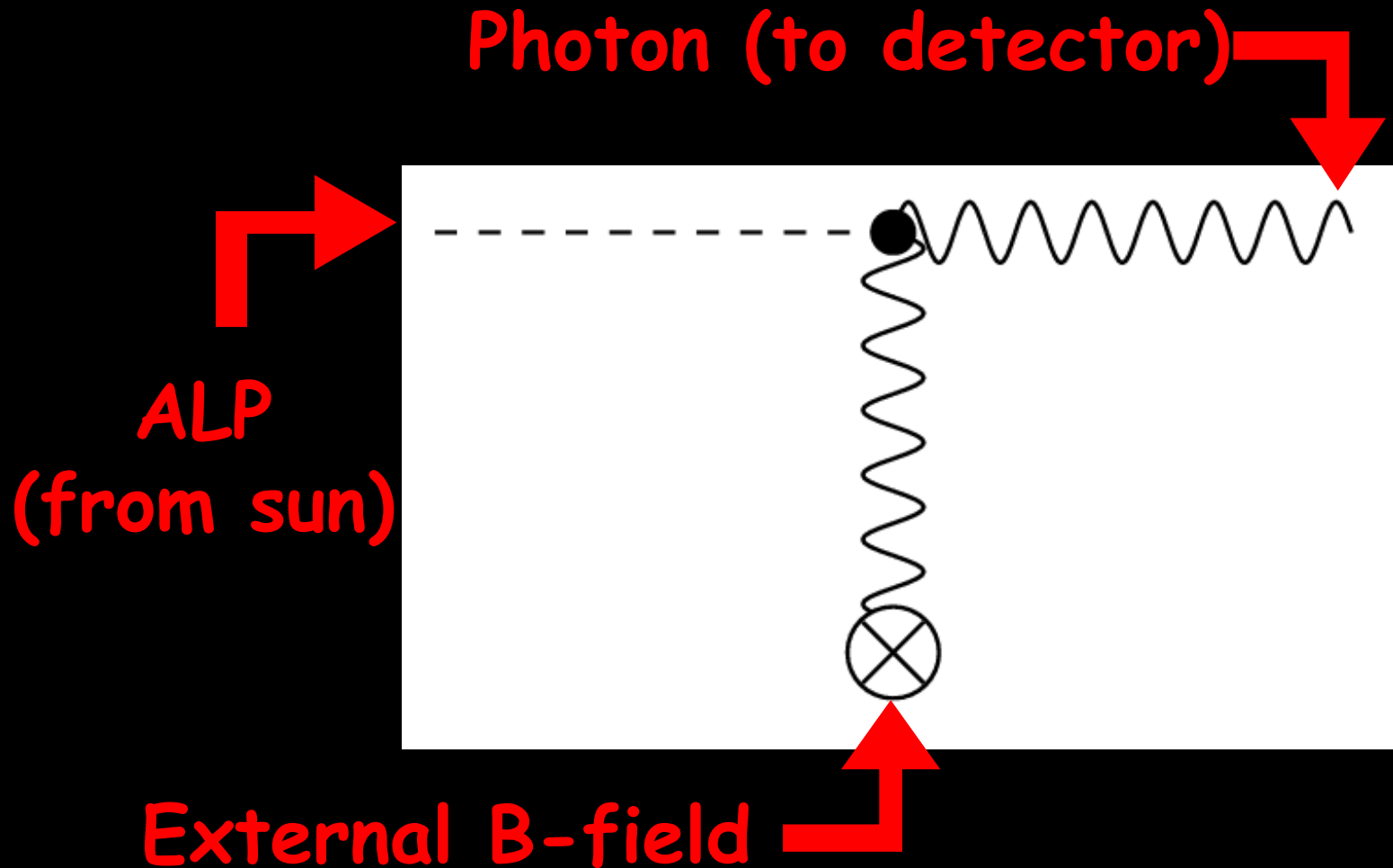
Bound from Star Lifetimes



Regeneration



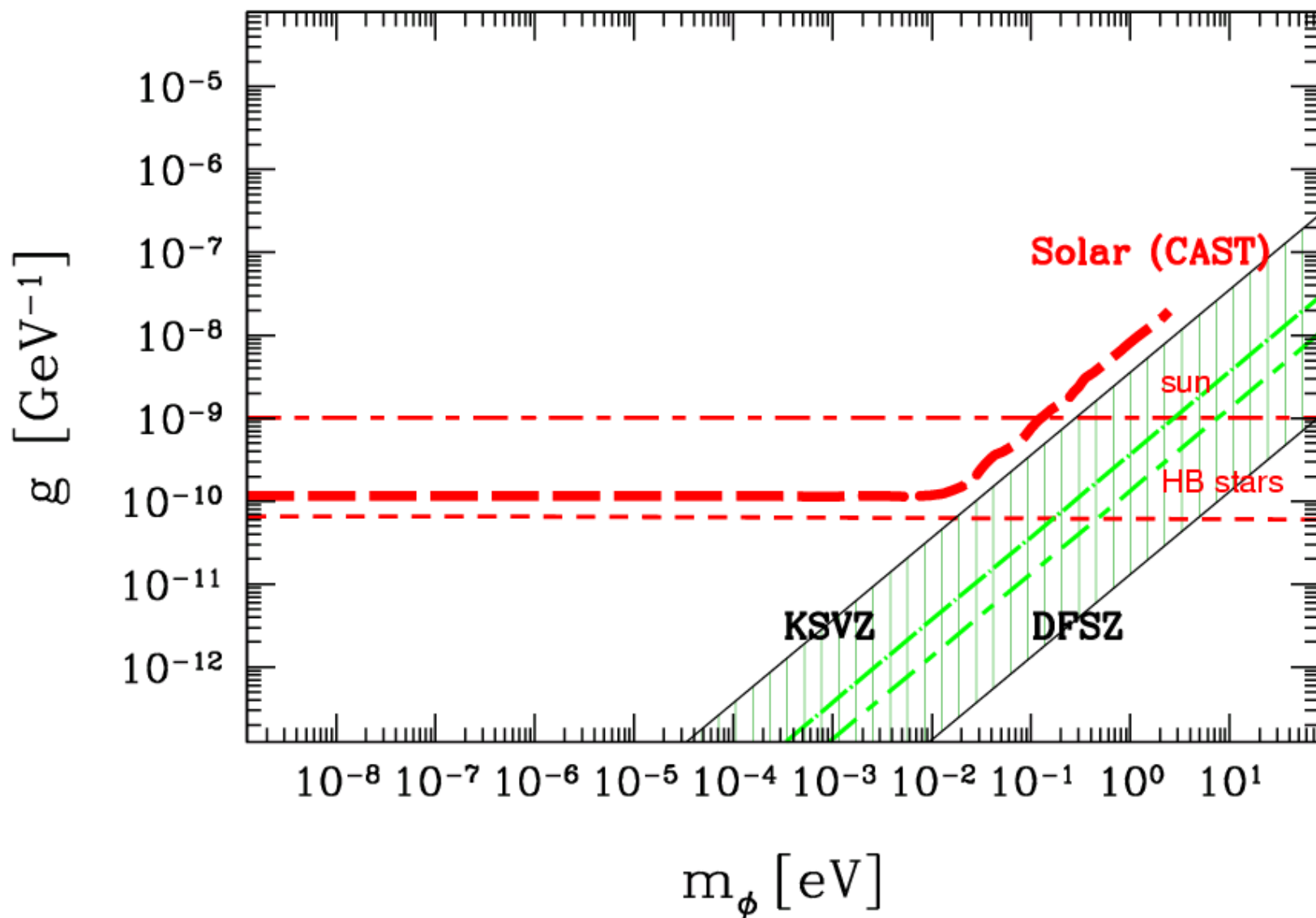
- Primakoff goes the other way around



CAST

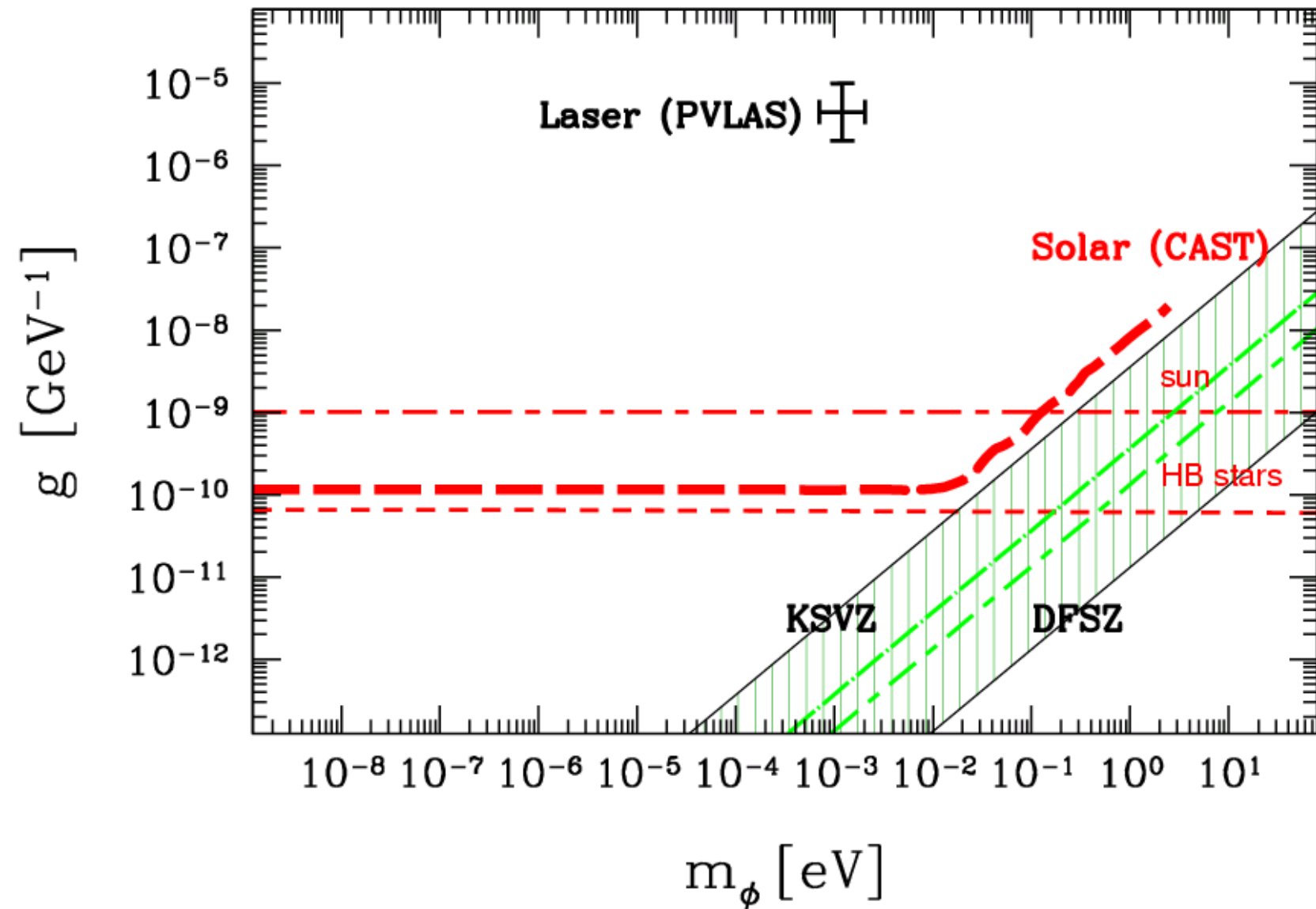


CAST bound



3. PVLAS

PVLAS Result



Problem



- ALP interpretation of PVLAS in severe conflict with astrophysical bounds

Can we reconcile these results?

4. Evading Astrophysical bounds

Be careful:
Highly Speculative!

Two Basic Ideas



- 1. Trap the ALPs in the sun (like γ 's)
(ALPs interact many times before leaving the sun)
 - Prevents excessive energy loss
 - Prevents detection via CAST
 - Smaller number of ALPs emitted
 - Emitted ALPs have lower energy
 - 2. Suppress production in the sun
-

Suppress Production



- Idea: In the center of the sun the environment is different from a lab environment.
 - High temperature
 - Large virtuality q^2
 - High density (compared to vacuum)
 - Large $F^{\mu\nu}$ in Primakoff prozess
 - High neutrino flux
-

Phenomenological Approach



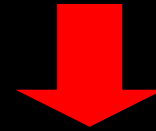
- Simplest phenomenological approach:
Make ALP-parameters environment dependent

$$m_a \rightarrow m_a(\text{environment}), \quad g \rightarrow g(\text{environment})$$



$$m_a > T$$

forbids production
kinematically



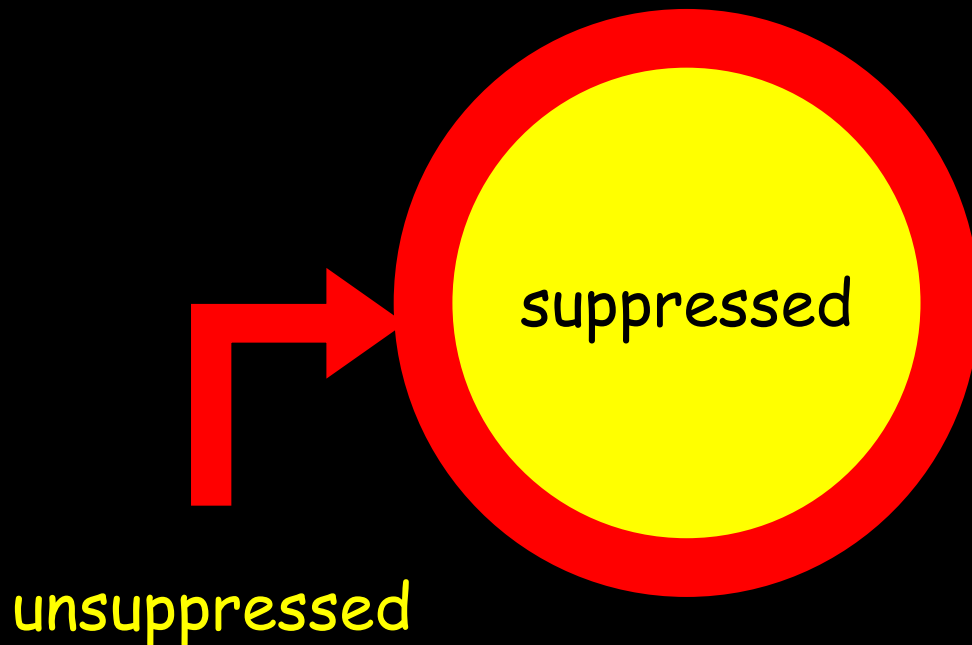
g small

suppresses production
via the coupling

Radial suppression



- Since $\rho, T, \langle F \rangle, j_\nu$ depend only on the radius this suppresses production up to a certain radius



How much suppression needed?



- The coupling compatible with PVLAS is $g_{\text{PVLAS}}^{-1} \sim 10^5 \text{GeV}$

- Lifetime argument: $g_{\text{life}}^{-1} \sim 10^{10} \text{GeV}$

$$\text{Production} \sim g^2 \quad \longrightarrow \quad S \sim \frac{g_{\text{life}}^2}{g_{\text{PVLAS}}^2} \sim 10^{-10}$$

- CAST: $g_{\text{CAST}}^{-1} \sim 10^{10} \text{GeV}$

$$\text{Production} \times \text{Regeneration} \sim g^4$$

$$\longrightarrow \quad S \sim \frac{g_{\text{life}}^4}{g_{\text{PVLAS}}^4} \sim 10^{-20}$$

Is the Sun Extreme?



• At 0% Radius: $T \sim 1.5 \cdot 10^7 \text{K} \approx 1200 \text{eV}$
 $\rho \sim 150 \text{ g/cm}^3$
 $\langle |q| \rangle \gtrsim 290 \text{eV}$

At 79% Radius: $T \sim 1.4 \cdot 10^6 \text{K} \approx 117 \text{eV}$
 $\rho \sim 9.8 \cdot 10^{-2} \text{g/cm}^3$
 $\langle |q| \rangle \gtrsim 9 \text{eV}$
 $S \sim 10^{-4}$

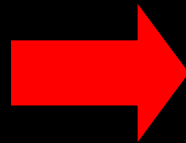
At 97% Radius: $T \sim 1.5 \cdot 10^5 \text{K} \approx 12.5 \text{eV}$
 $\rho \sim 3 \cdot 10^{-3} \text{g/cm}^3$
 $\langle |q| \rangle \gtrsim 1.4 \text{eV}$
 $S \sim 10^{-20}$

 The absolute values for T, ρ in the sun are far from extreme!

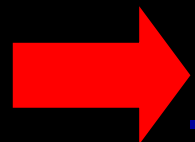
Compared to PVLAS



- Density up to $\lesssim 2 \cdot 10^{-5} \text{g/cm}^3$
- Temperature $T \lesssim 300\text{K} \sim 0.025\text{eV}$
- $|q| \sim 10^{-6}\text{eV}$

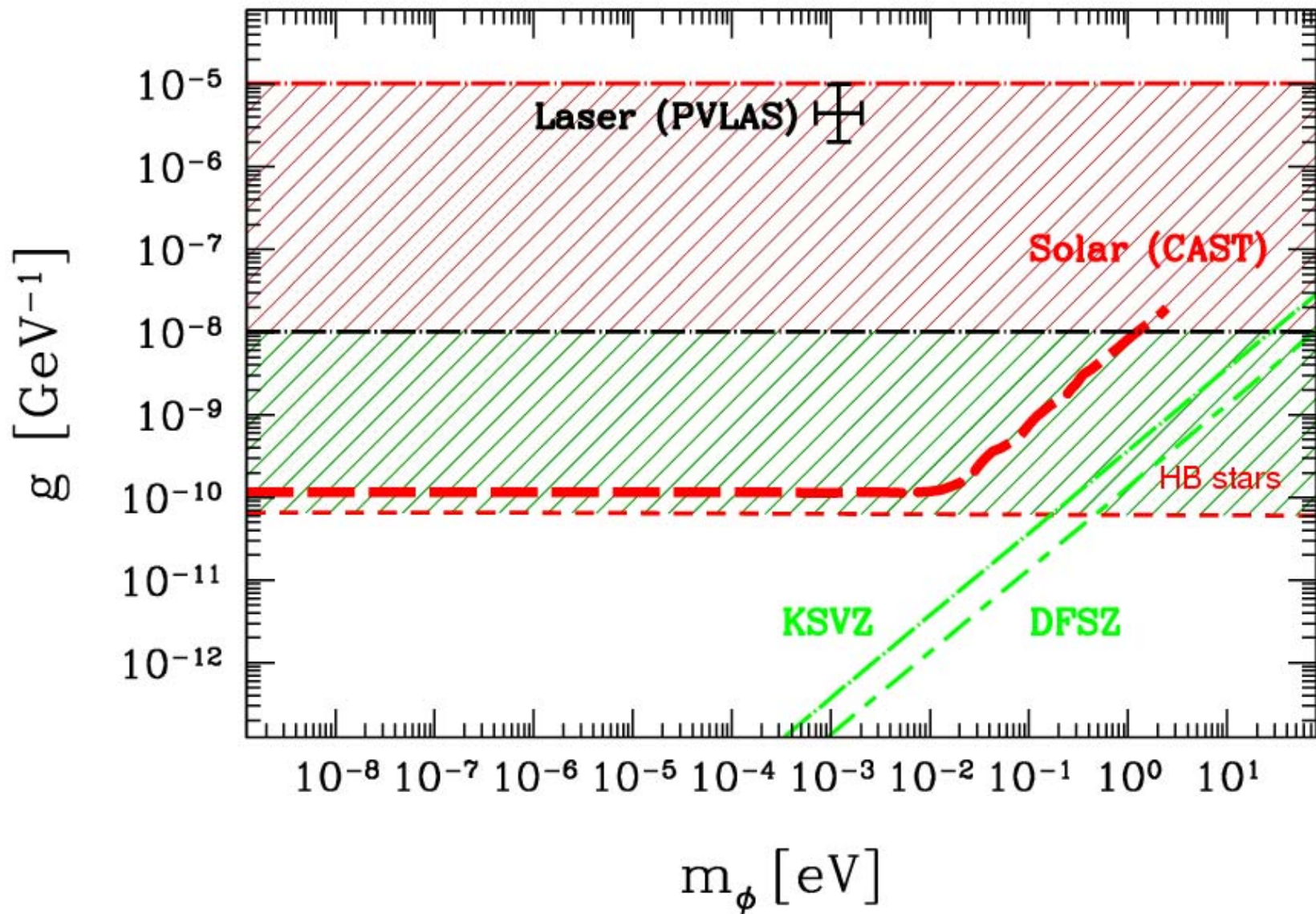


Compared to the
environment of PVLAS:
The sun is hot and dense!
And the average $|q|$ is high.



Room for exotic possibilities!!!

Wiggling Room



g^2

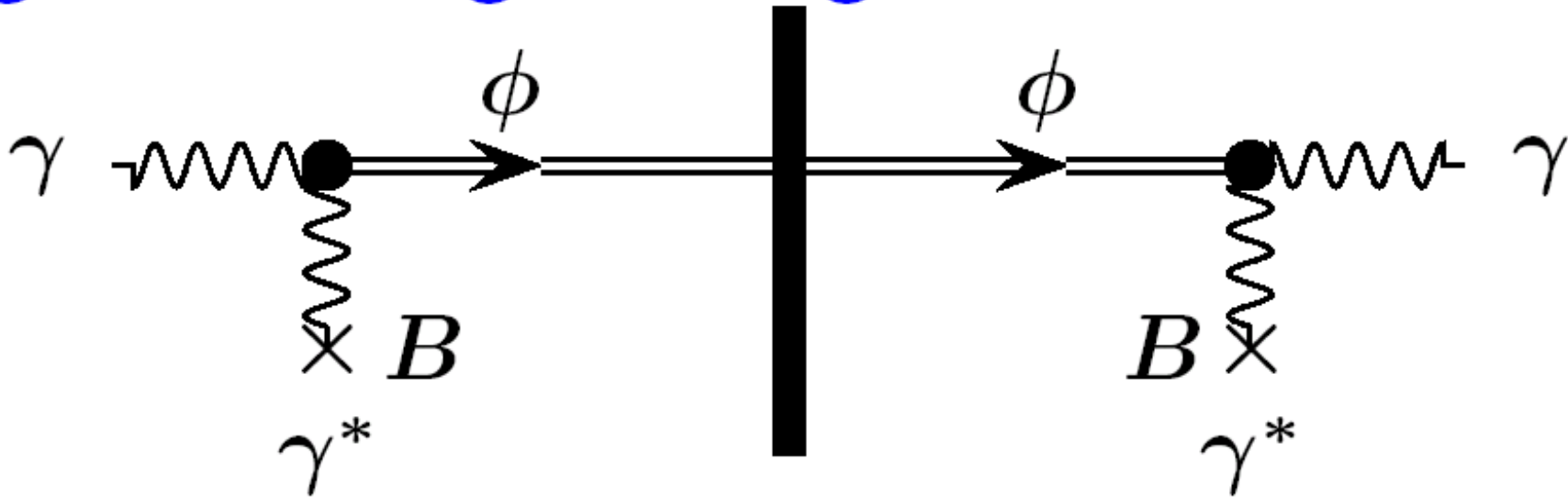
We need
Lab Experiments

5. The Future: Light Shining through Walls

Light shining through walls



“Light shining through a wall”

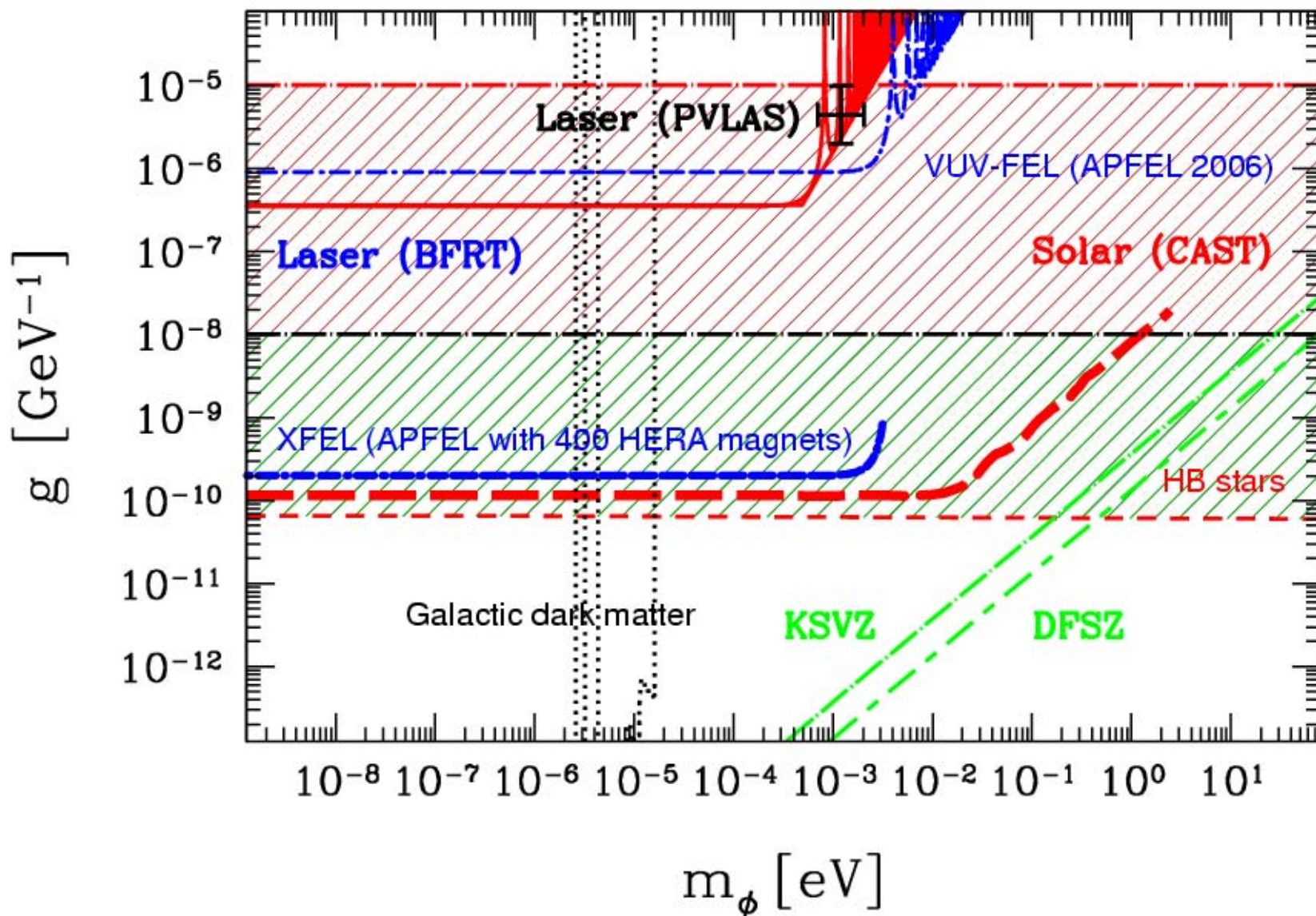


- VUV-FEL + Accelerator Magnets
- XFEL + Hera Magnets

An Accelerator Magnet



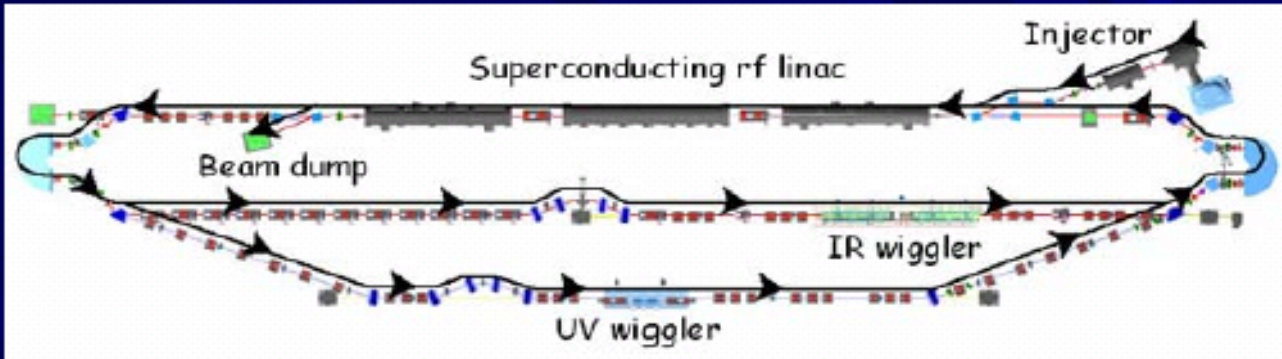
Can Test PVLAS



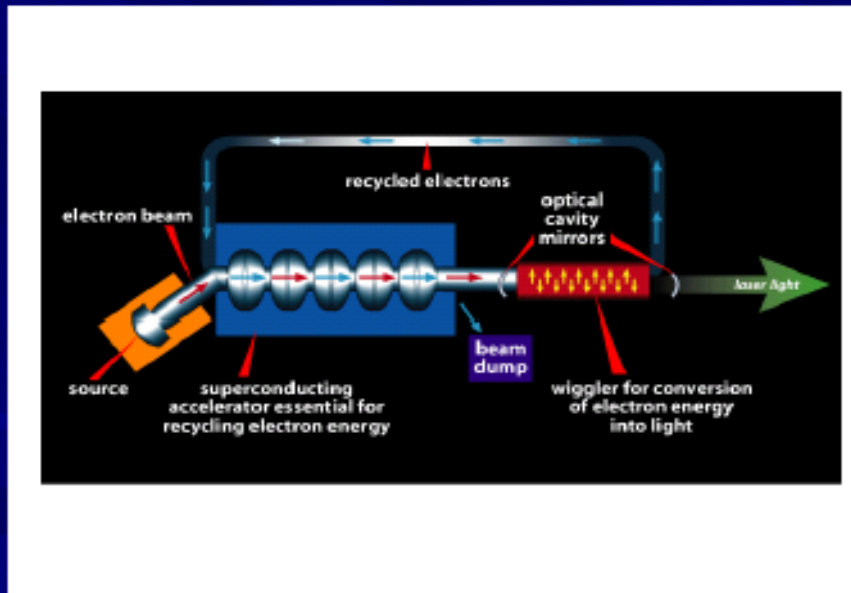
The competition is'nt sleeping...



JLAB FEL setup I: regeneration experiment



"parasitic"



magnet

2 T; 1 m (?)

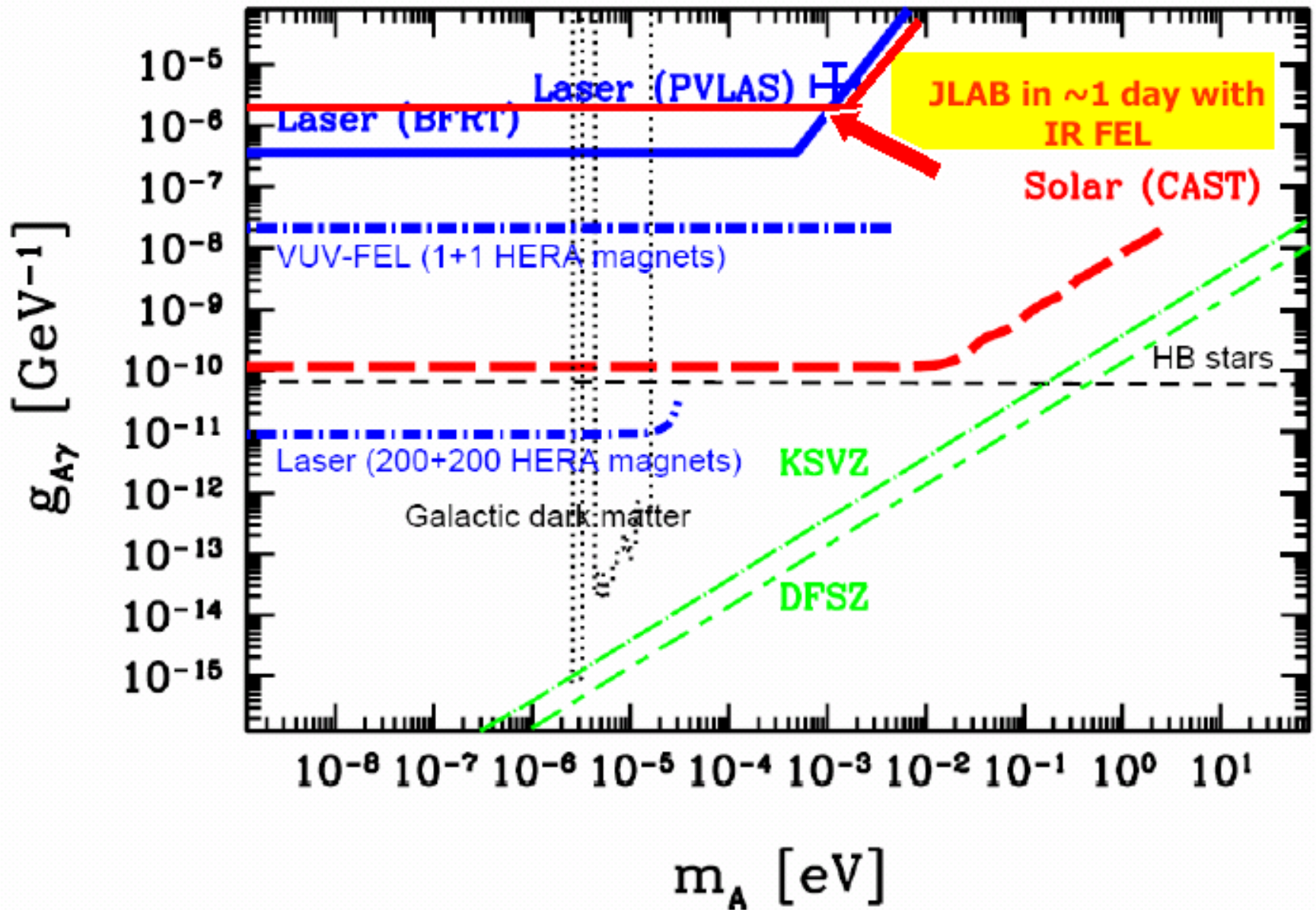


detector

ϕ 's produced at JLAB FEL

light shield

Their sensitivity...



6. Conclusions

Conclusions



- Axions are a good solution to the strong CP problem
- Astrophysics provide strong bounds on light bosons coupled to two photons
- PVLAS may have detected an ALP but is in conflict with astrophysics
- Might be possible to evade astrophysical bounds

Near future lab experiments
are able to
test interesting regions for ALPs



In motion everything is...
Difficult to see is the future...
Uncertain it is...
...exciting it is.