

Matter-Gluon interaction

Axel Maas

4th of November 2010
The Many Faces of QCD
Ghent
Belgium

FWF

**UNI
GRAZ**

(Scalar) Matter-Gluon interaction

Axel Maas

4th of November 2010
The Many Faces of QCD
Ghent
Belgium

FWF

**UNI
GRAZ**

(Scalar) Matter-Gluon interaction

PRELIMINARY

Axel Maas

4th of November 2010
The Many Faces of QCD
Ghent
Belgium

FWF

UNI
GRAZ

Why scalar-gluon interactions?

Why scalar-gluon interactions?

- **Aim: Methods to answer physics questions**

Why scalar-gluon interactions?

- **Aim: Methods to answer physics questions**
- **Use a combination of lattice and functional methods**
 - **Lattice provides (comparatively) good reliability**
 - **Functional methods can go where lattice cannot**
 - **Density, massless fermions, real time, disparate energy scales**

Why scalar-gluon interactions?

- **Aim: Methods to answer physics questions**
- **Use a combination of lattice and functional methods**
 - **Lattice provides (comparatively) good reliability**
 - **Functional methods can go where lattice cannot**
 - **Density, massless fermions, real time, disparate energy scales**
 - **Simplest common objects: Correlation functions of the elementary particles**

Why scalar-gluon interactions?

- **Aim: Methods to answer physics questions**
- **Use a combination of lattice and functional methods**
 - **Lattice provides (comparatively) good reliability**
 - **Functional methods can go where lattice cannot**
 - **Density, massless fermions, real time, disparate energy scales**
 - **Simplest common objects: Correlation functions of the elementary particles**
 - **Structure less complicated for scalars**

Why scalar-gluon interactions?

- **Aim: Methods to answer physics questions**
- **Use a combination of lattice and functional methods**
 - **Lattice provides (comparatively) good reliability**
 - **Functional methods can go where lattice cannot**
 - **Density, massless fermions, real time, disparate energy scales**
 - **Simplest common objects: Correlation functions of the elementary particles**
 - **Structure less complicated for scalars**
 - **But also much progress for fermions**

Why scalar-gluon interactions?

- **Aim: Answer physics questions**

Why scalar-gluon interactions?

- **Aim: Answer physics questions**
- **Scalars as role-model for fermions to understand confinement**
 - **Wilson loops blind to the Lorentz structure**
 - **No interference of chiral symmetry**

Why scalar-gluon interactions?

- **Aim: Answer physics questions**
- **Scalars as role-model for fermions to understand confinement**
 - Wilson loops blind to the Lorentz structure
 - No interference of chiral symmetry
- **Scalars could play a role in, or beyond, the standard model**
 - Higgs and generalizations, sfermions,...

Why scalar-gluon interactions?

- **Aim: Answer physics questions**
- **Scalars as role-model for fermions to understand confinement**
 - Wilson loops blind to the Lorentz structure
 - No interference of chiral symmetry
- **Scalars could play a role in, or beyond, the standard model**
 - Higgs and generalizations, sfermions,...
- **Field theoretically important**
 - Higgs mechanism and Higgs vs. confinement
 - Triviality in complex theories

Interesting systems

- **Quenched scalars**

Interesting systems

- **Quenched scalars**
 - **Fundamental vs. adjoint**

Interesting systems

- **Quenched scalars**
 - **Fundamental vs. adjoint**
 - **Is the behavior of the Wilson potential manifest in (low-order) correlation functions?**
 - **Propagators, 3-point-functions,...**
 - **Mass dependence?**

Interesting systems

- **Quenched scalars**
 - **Fundamental vs. adjoint**
 - **Is the behavior of the Wilson potential manifest in (low-order) correlation functions?**
 - Propagators, 3-point-functions,...
 - Mass dependence?
- **Unquenched fundamental scalars**

Interesting systems

- **Quenched scalars**
 - **Fundamental vs. adjoint**
 - **Is the behavior of the Wilson potential manifest in (low-order) correlation functions?**
 - Propagators, 3-point-functions,...
 - Mass dependence?
- **Unquenched fundamental scalars**
 - **Is the the Higgs mechanism and confinement different?**

Quenched scalars

- **Minimal Landau gauge results**

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**
 - **Single scalar function**
 - **No distinction between a mass function and a wave-function as for fermions**

Quenched scalars

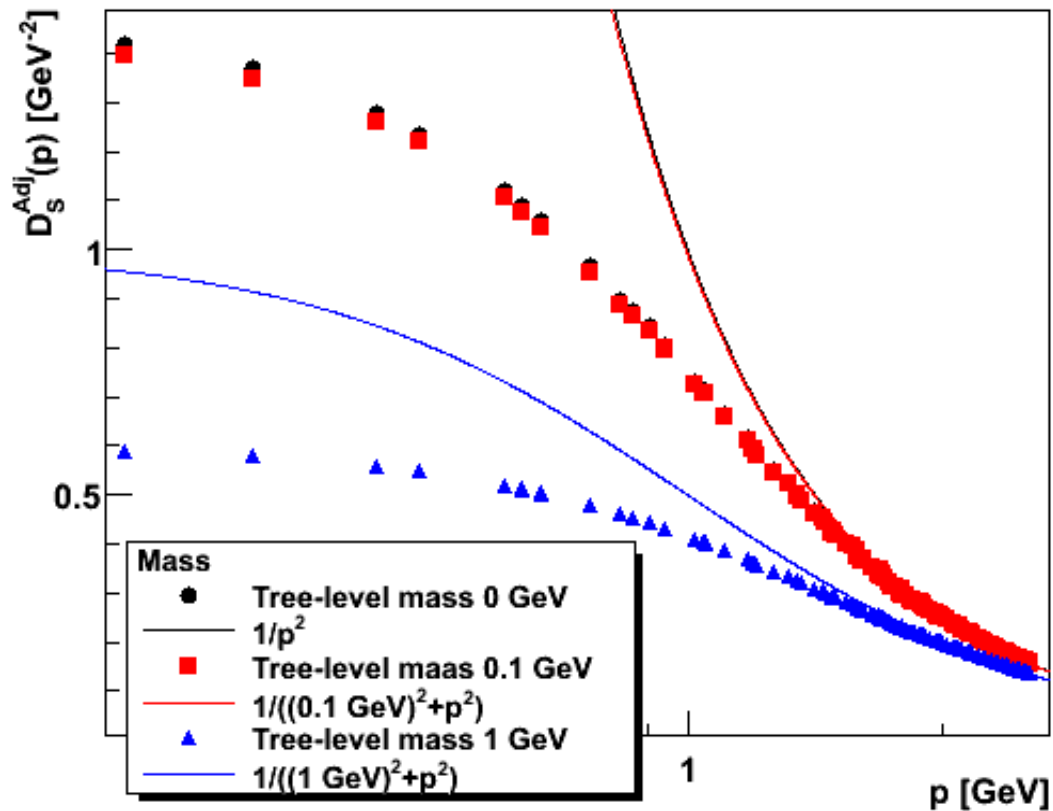
- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**
 - **Single scalar function**
 - **No distinction between a mass function and a wave-function as for fermions**
 - **Two independent renormalizations necessary**
 - **Mass is quadratic divergent – necessary also in lower dimensions**
 - **Renormalize to tree-level at 2 GeV** [Maas, 2010]

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**
 - **Single scalar function**
 - **No distinction between a mass function and a wave-function as for fermions**
 - **Two independent renormalizations necessary**
 - **Mass is quadratic divergent – necessary also in lower dimensions**
 - **Renormalize to tree-level at 2 GeV** [Maas, 2010]
- **Compare two, three, and four dimensions**
 - **Two scaling-like, four decoupling-like**

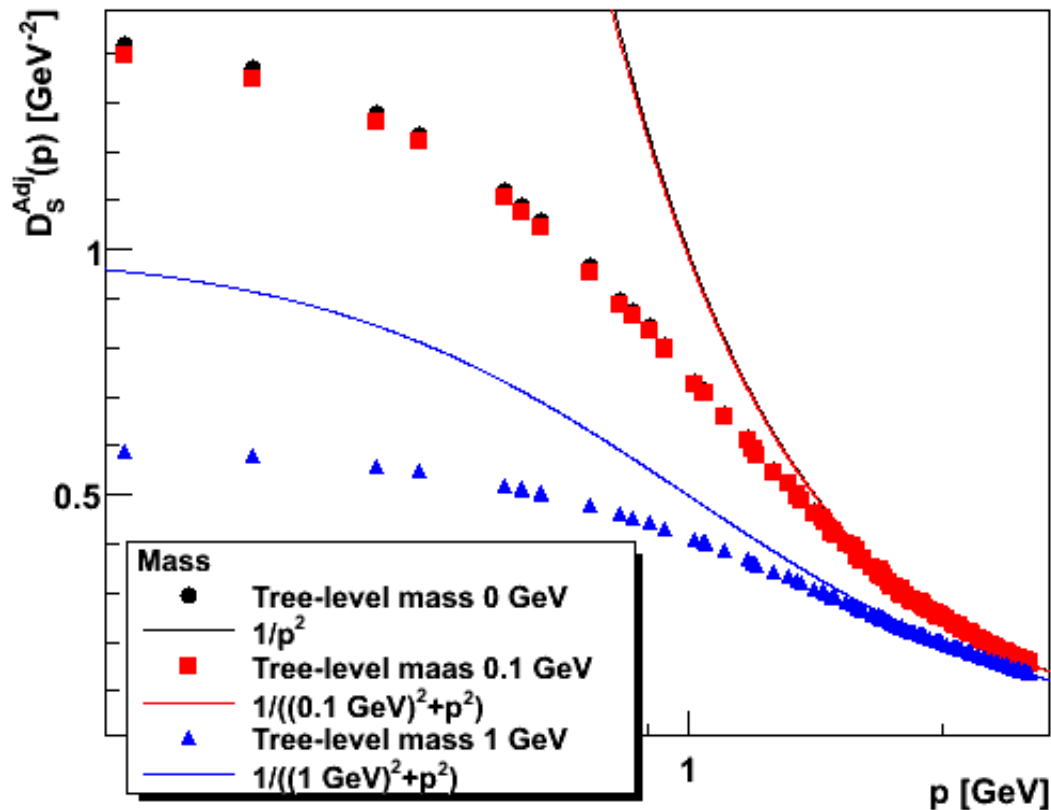
2d: Adjoint vs. Fundamental

Adjoint scalar propagator



2d: Adjoint vs. Fundamental

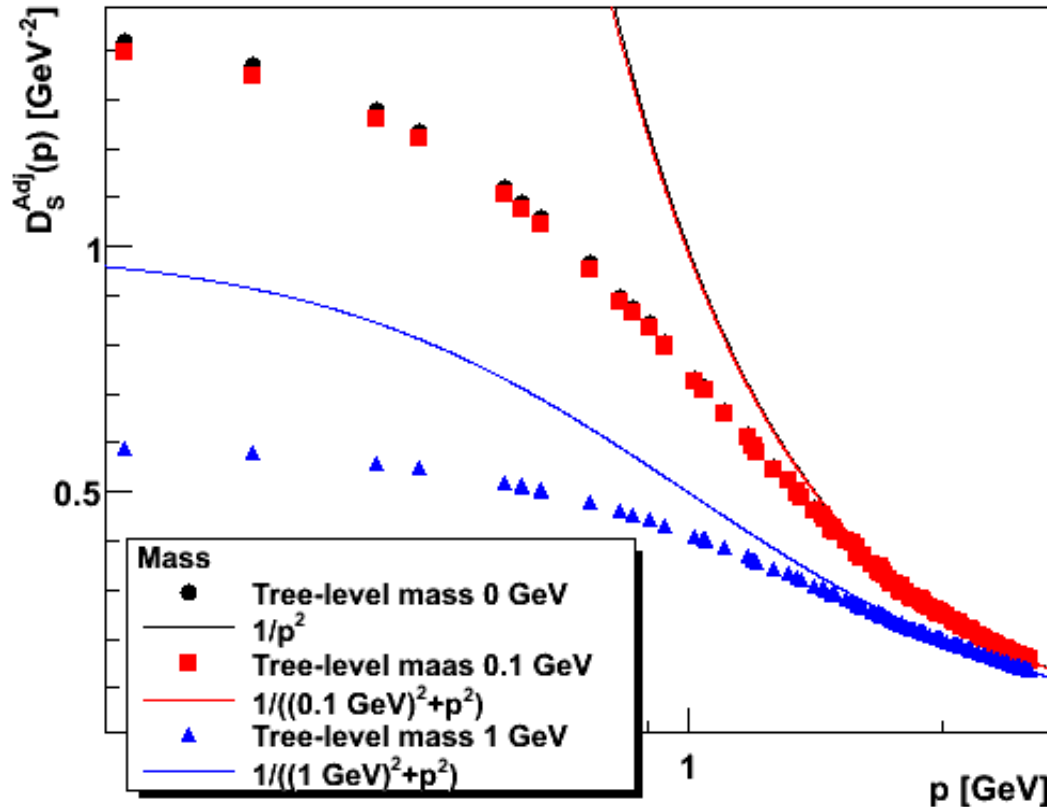
Adjoint scalar propagator



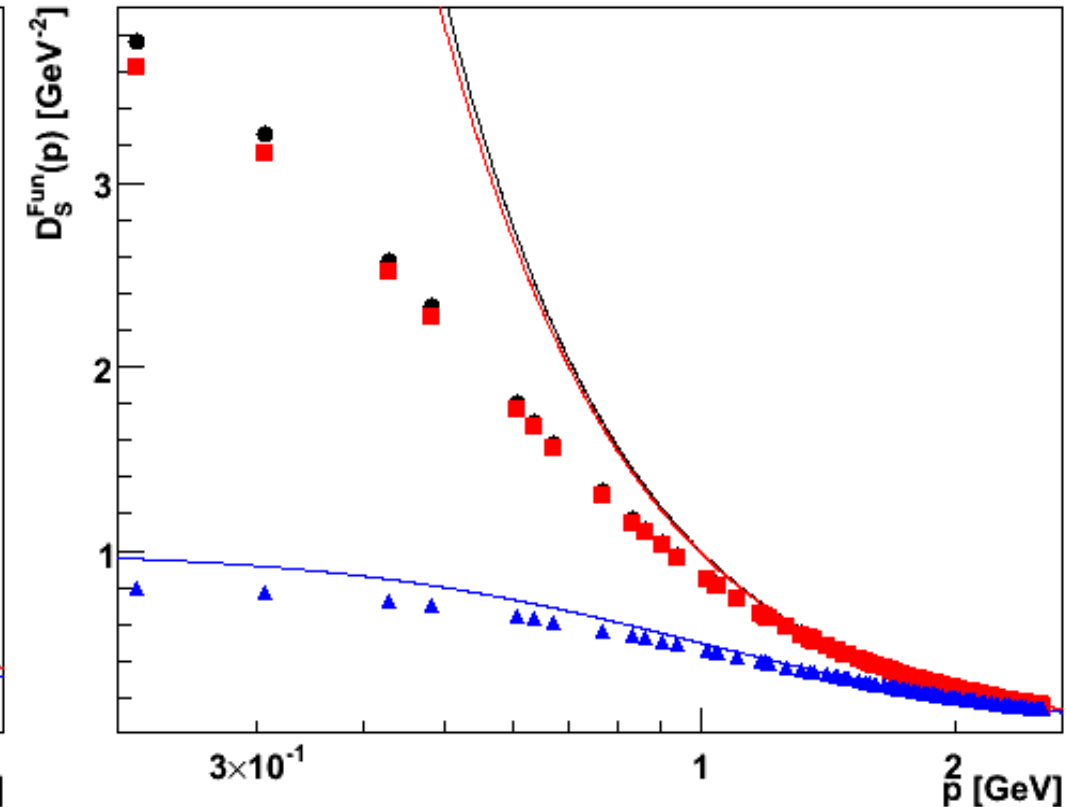
- Screening-mass unequal renormalized mass
 - Mass-dependent screening mass generation

2d: Adjoint vs. Fundamental

Adjoint scalar propagator



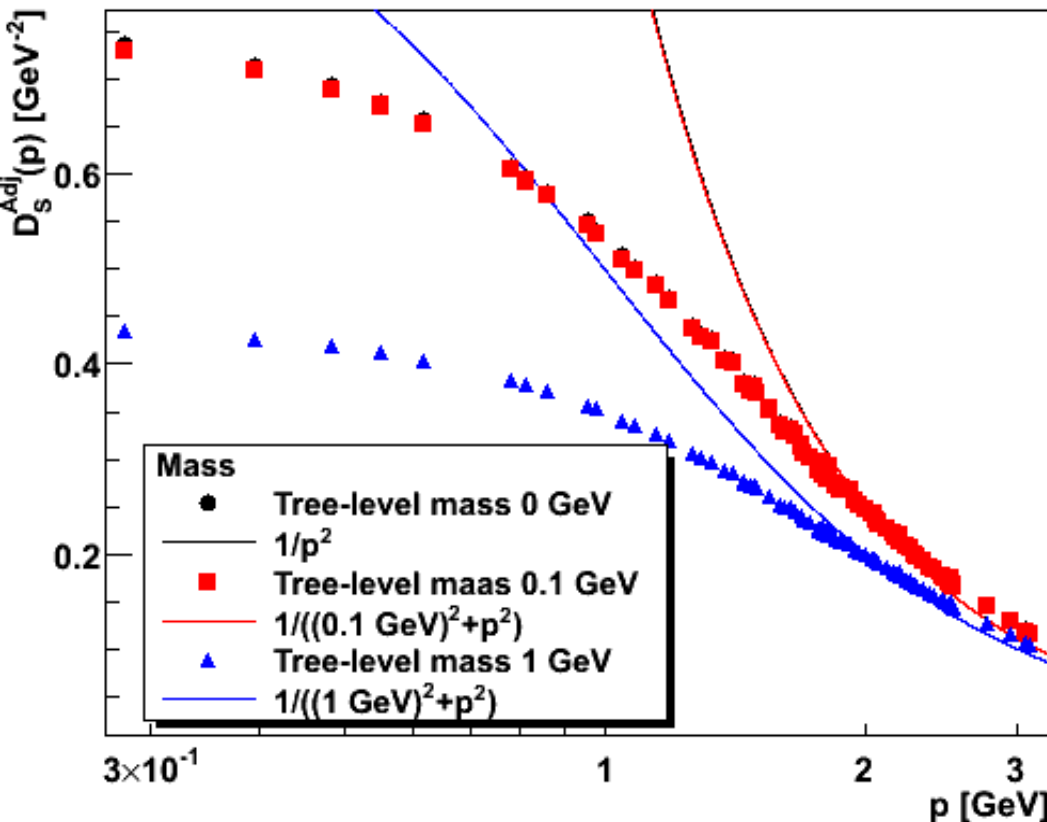
Fundamental scalar propagator



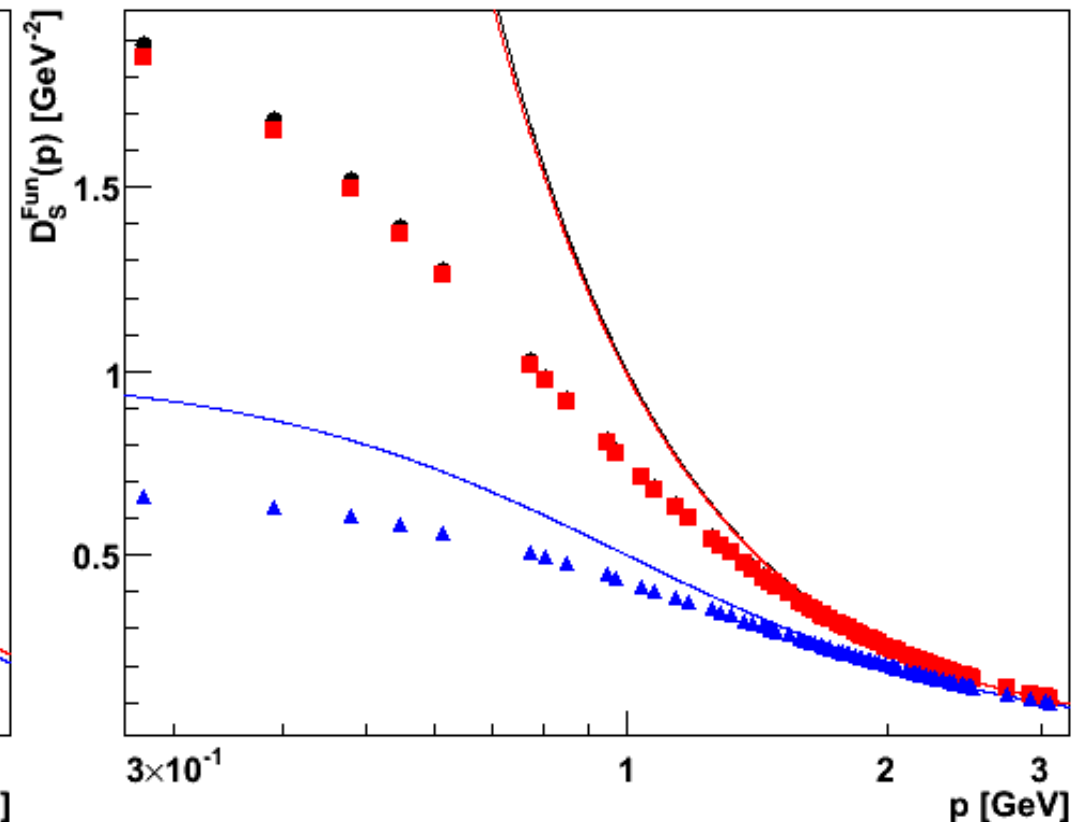
- Screening-mass unequal renormalized mass
 - Mass-dependent screening mass generation
- Fundamental similar, but possibly different IR slope

3d: Adjoint vs. Fundamental

Adjoint scalar propagator



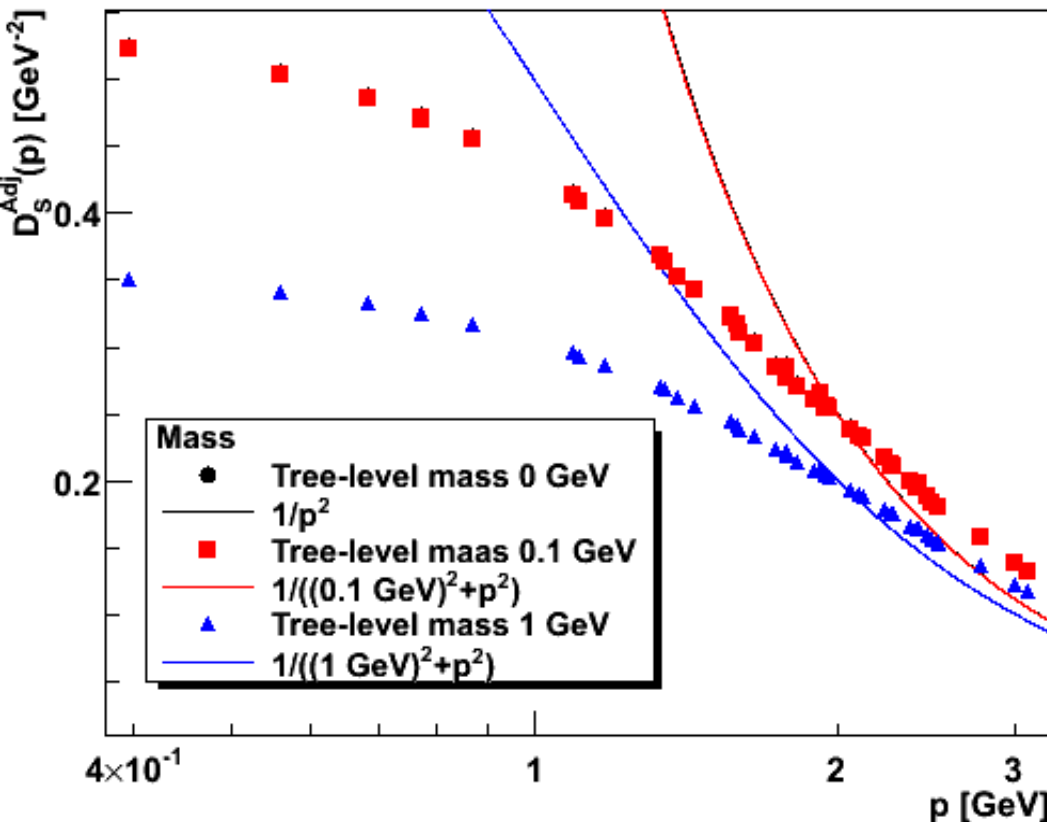
Fundamental scalar propagator



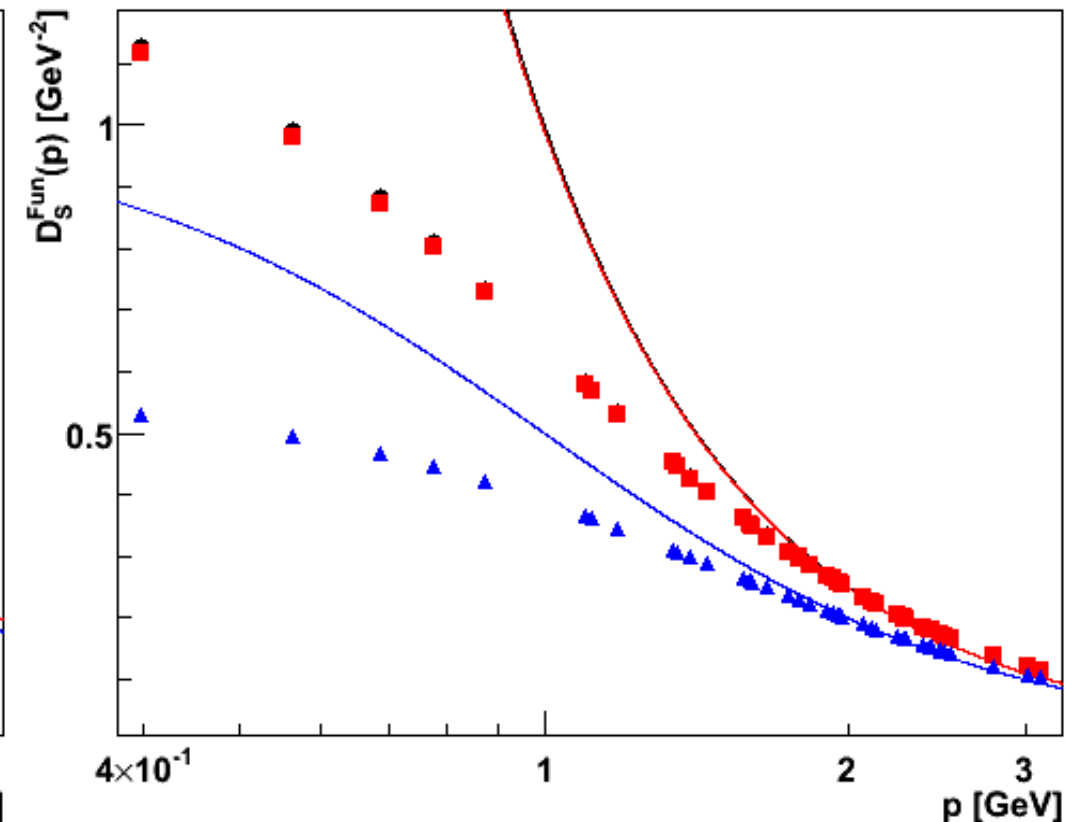
- Screening masses larger
- Slope difference less pronounced
- More UV modifications

4d: Adjoint vs. Fundamental

Adjoint scalar propagator



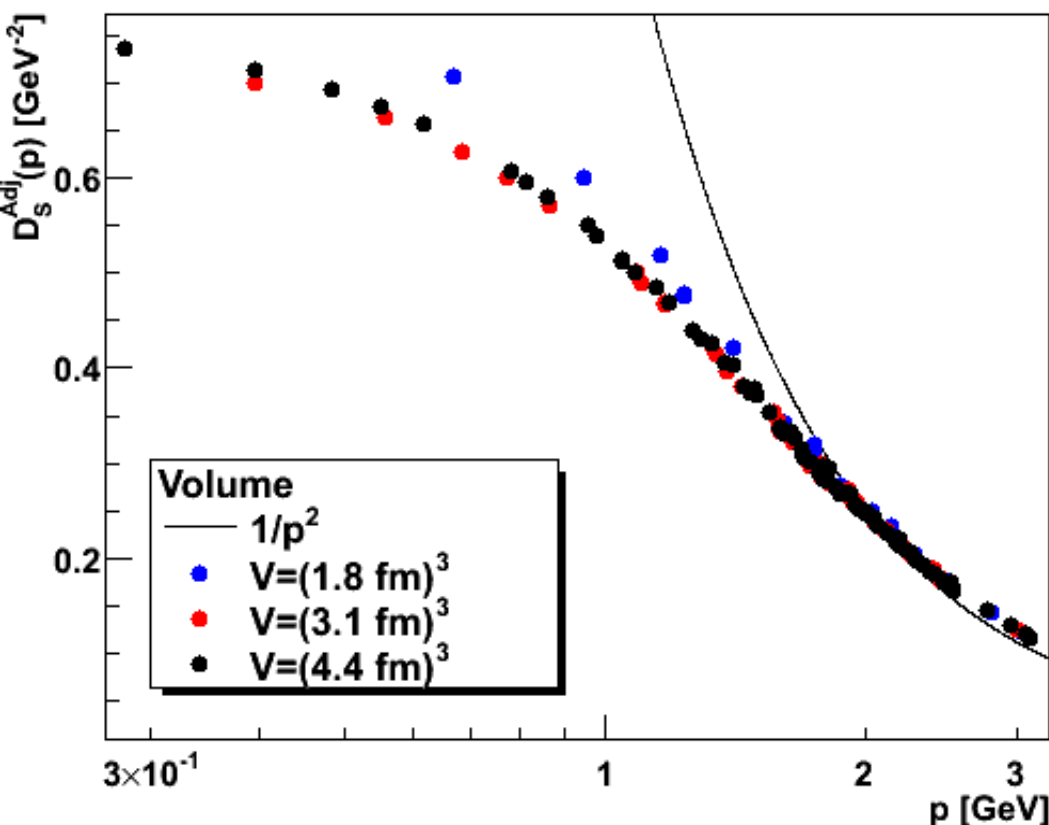
Fundamental scalar propagator



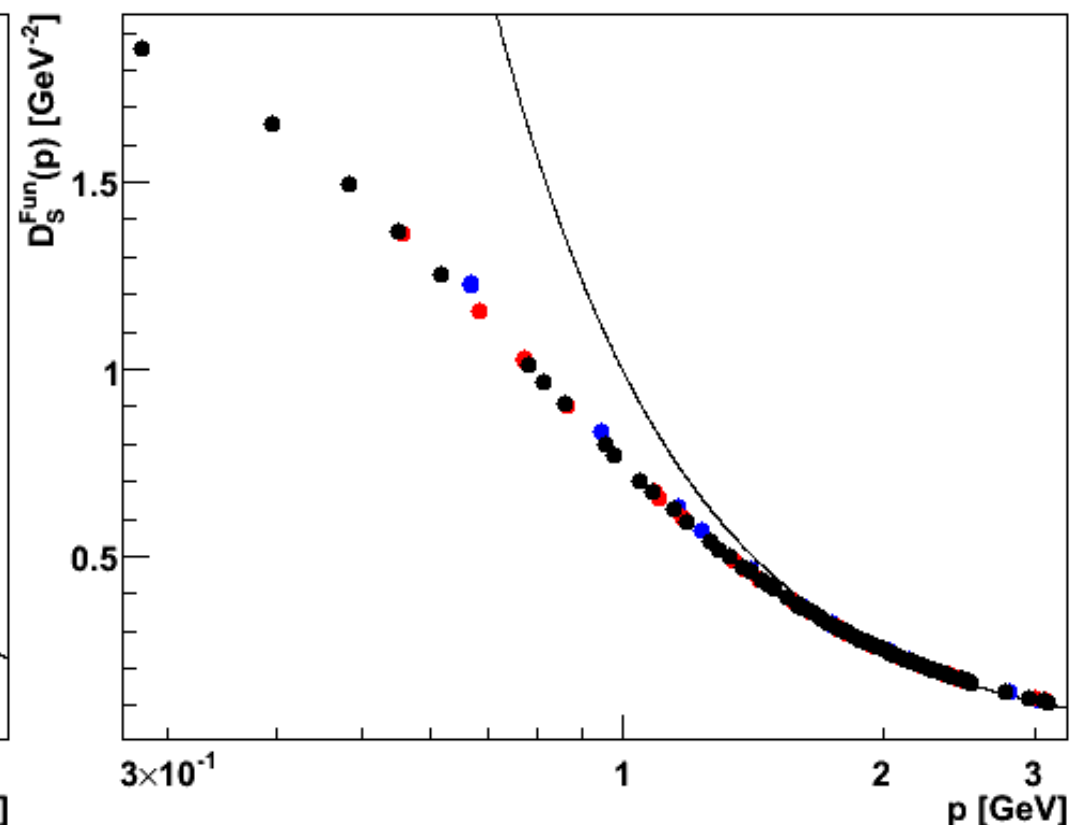
- Screening masses even larger
- Significant ultraviolet modifications
- Slope difference less pronounced

Volume dependence mass zero

Adjoint scalar propagator



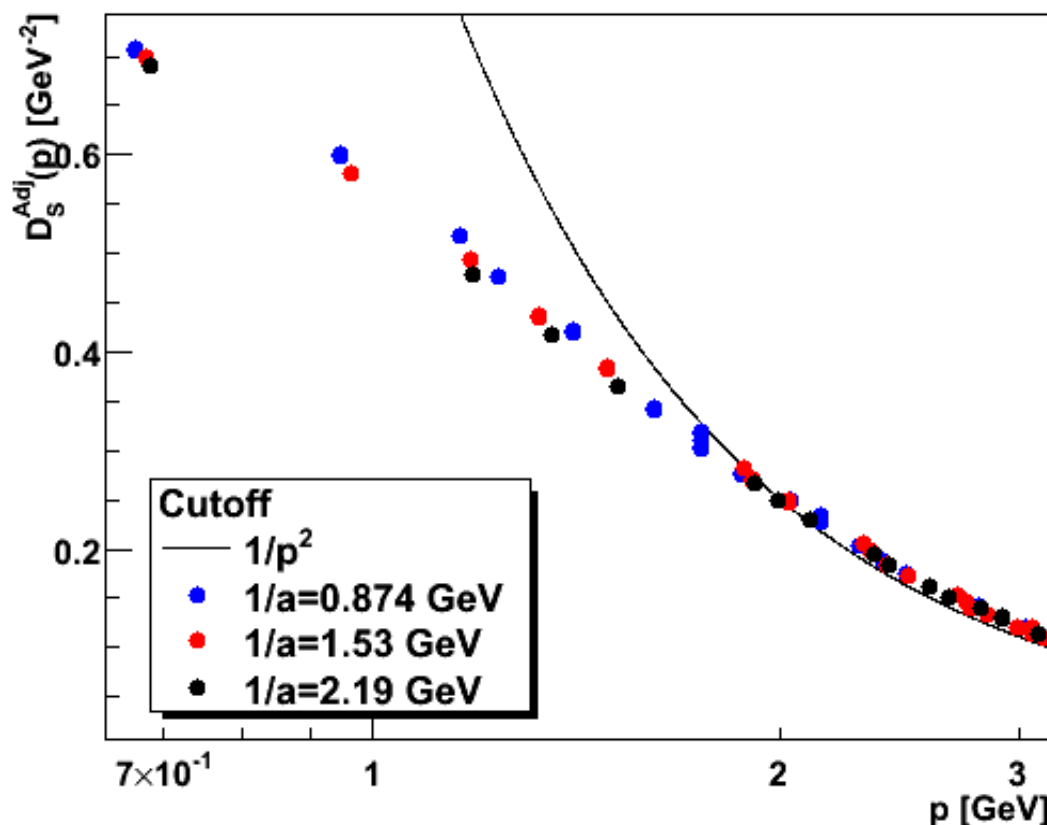
Fundamental scalar propagator



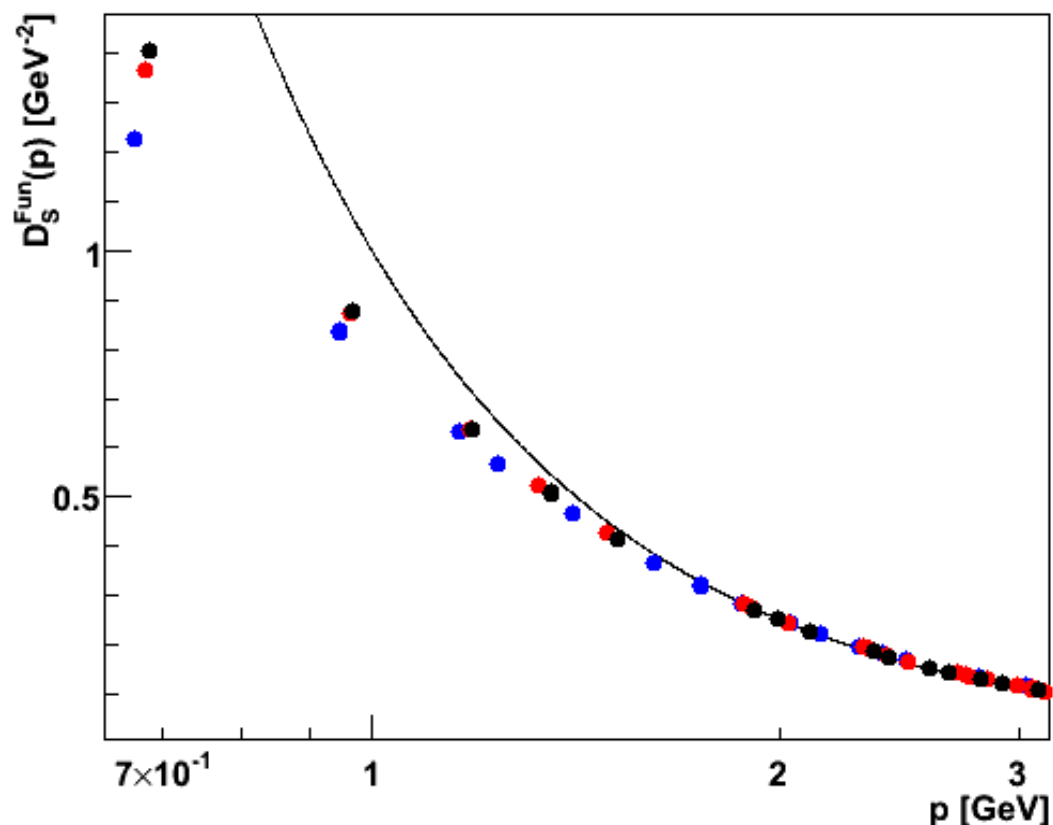
- No systematic volume effects (yet?)
- Adjoint scalars stronger affected
- Larger masses show less effect

Cutoff dependence mass zero

Adjoint scalar propagator



Fundamental scalar propagator



- Little effect for the adjoint
- Some systematic effect for fundamental
- Requires detailed investigations

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**
- **2-scalar-gluon vertex**

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**
- **2-scalar-gluon vertex**
 - **Only one relevant tensor structure**
 - **Like ghost-gluon vertex**
 - **But no non-renormalization theorem**

Quenched scalars

- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**
- **2-scalar-gluon vertex**
 - **Only one relevant tensor structure**
 - **Like ghost-gluon vertex**
 - **But no non-renormalization theorem**
 - **Only one renormalization necessary**
 - **Renormalized at an asymmetric point**

Quenched scalars

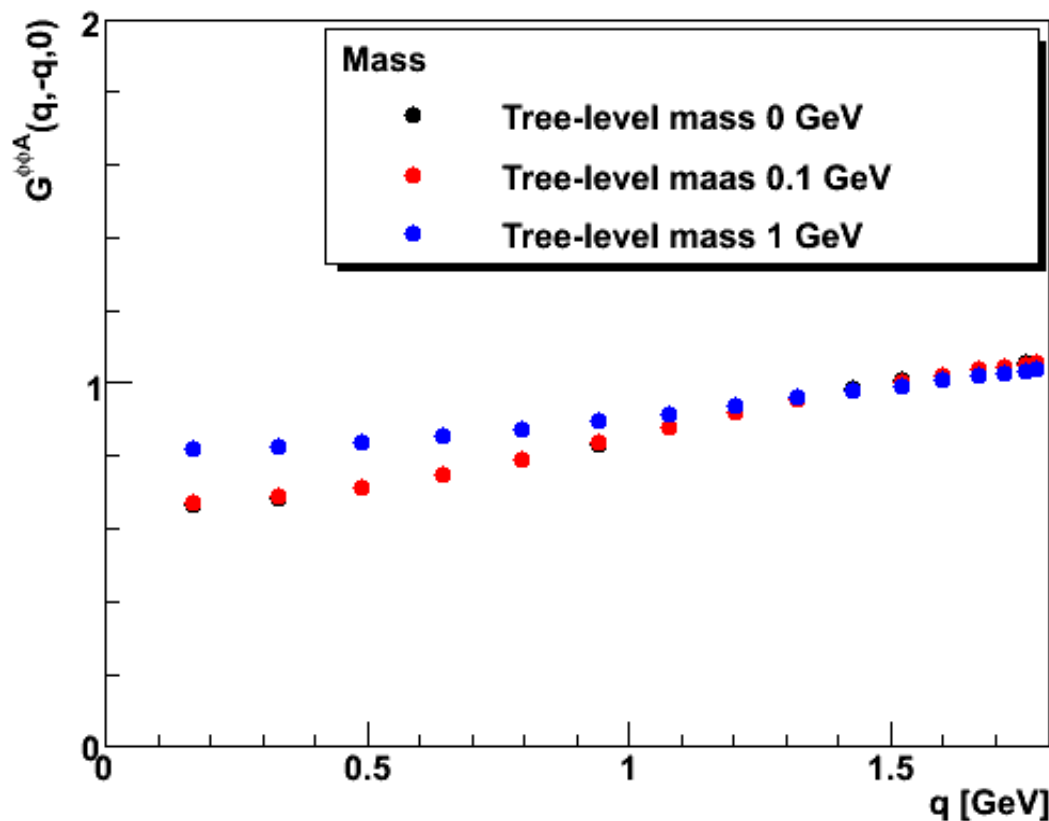
- **Minimal Landau gauge results**
- **Tree-level mass dependence**
- **Propagator**
- **2-scalar-gluon vertex**
 - **Only one relevant tensor structure**
 - **Like ghost-gluon vertex**
 - **But no non-renormalization theorem**
 - **Only one renormalization necessary**
 - **Renormalized at an asymmetric point**
 - **Configuration with zero gluon momentum**
 - **Symmetric and orthogonal similar**

2d: Gluon-2-scalar vertex

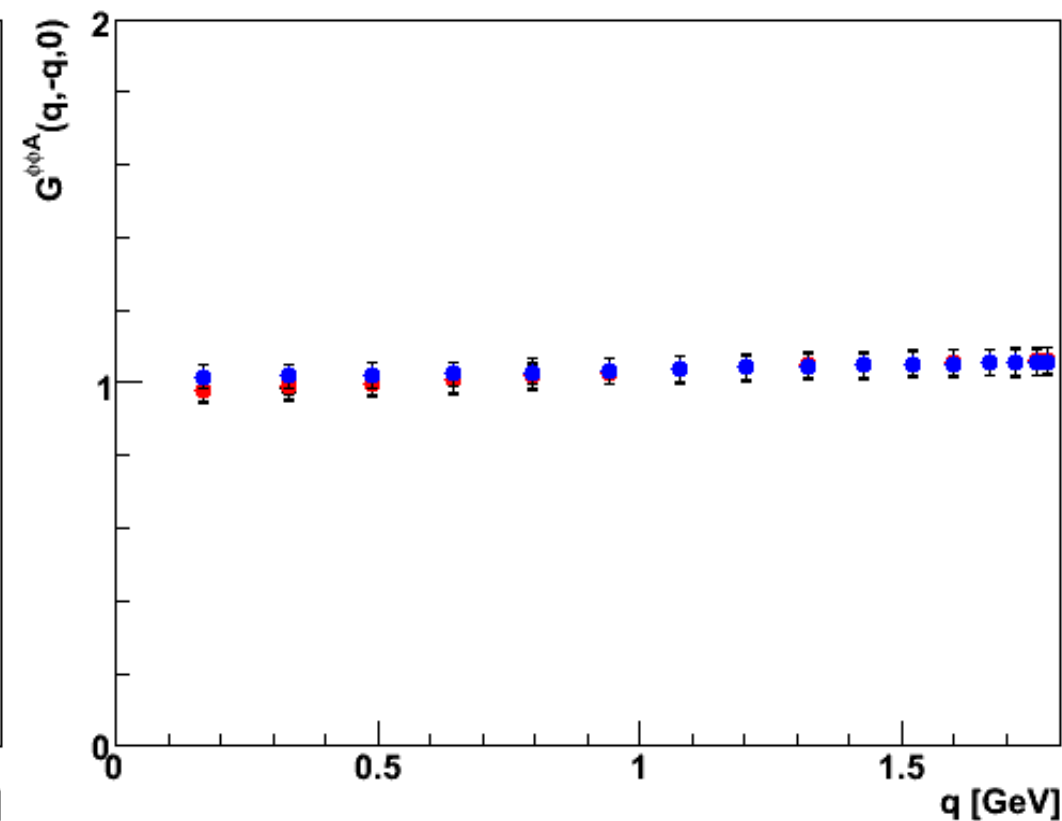
2d, $L=7.5$ fm, $a=0.22$ fm

[Maas unpublished]

Gluon-2-adjoint-scalar vertex, soft point



Gluon-2-fundamental-scalar vertex, soft point



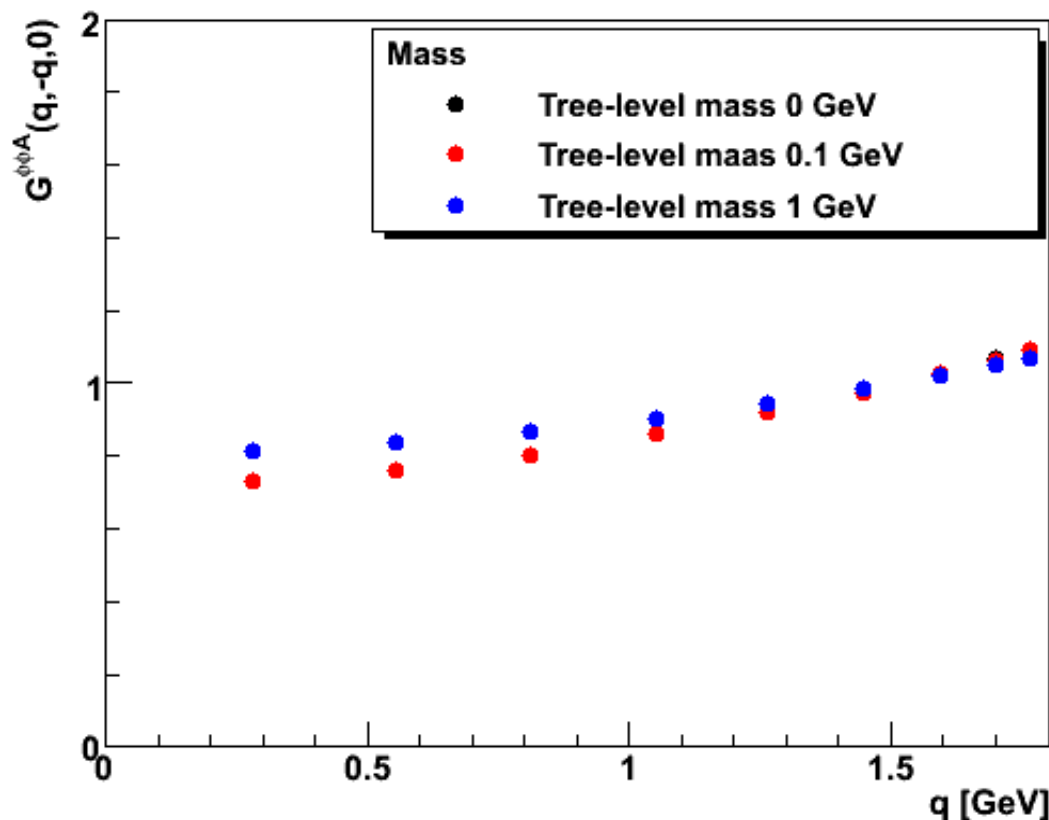
- **Almost no difference to tree-level (=1)**
 - Same for vanishing gluon/orthogonal scalar momenta
- **No divergences**

3d: Gluon-2-scalar vertex

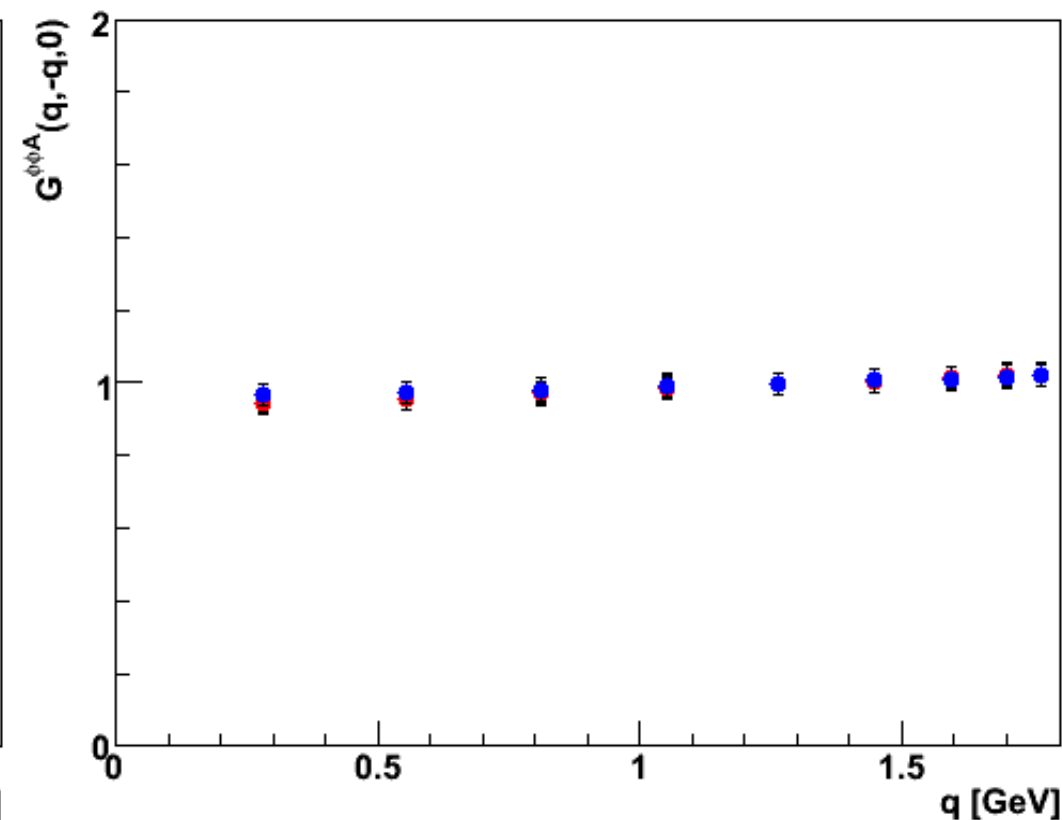
3d, $L=4.4$ fm, $a=0.22$ fm

[Maas unpublished]

Gluon-2-adjoint-scalar vertex, soft point



Gluon-2-fundamental-scalar vertex, soft point



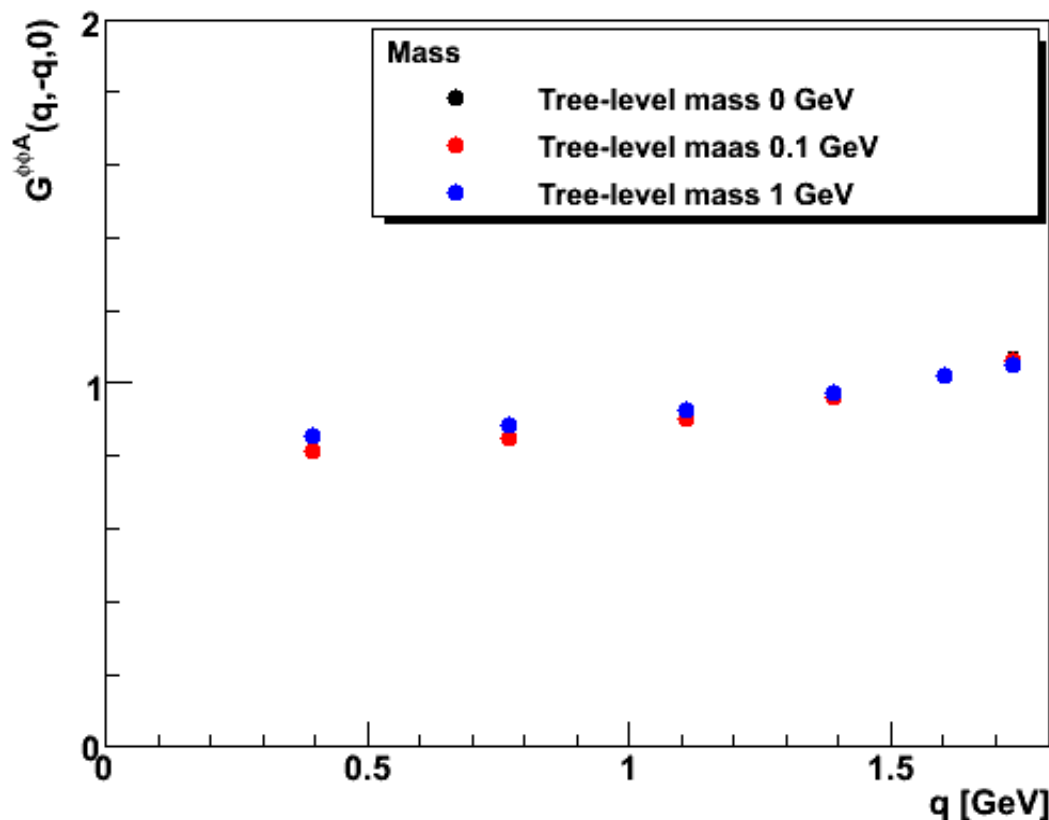
- **Very similar to two dimensions**
- **Some infrared suppression in the adjoint case**
- **Largely independent on tree-level mass**

4d: Gluon-2-scalar vertex

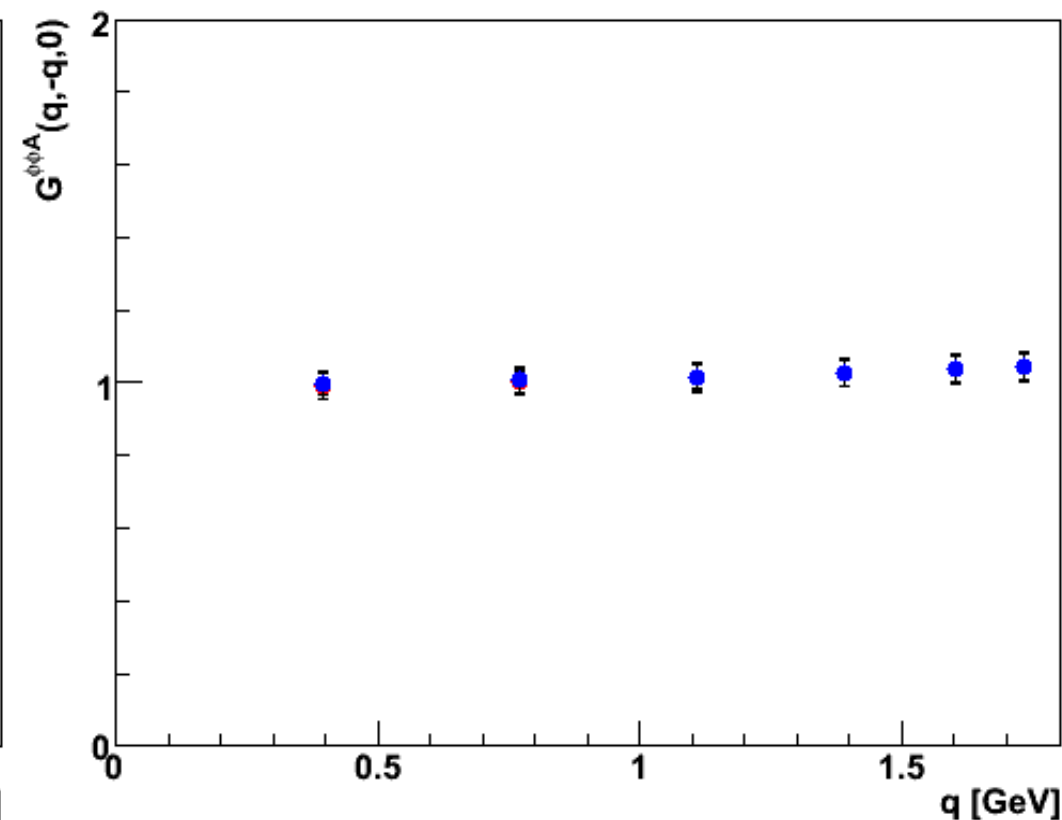
4d, $L=3.1$ fm, $a=0.22$ fm

[Maas unpublished]

Gluon-2-adjoint-scalar vertex, soft point



Gluon-2-fundamental-scalar vertex, soft point



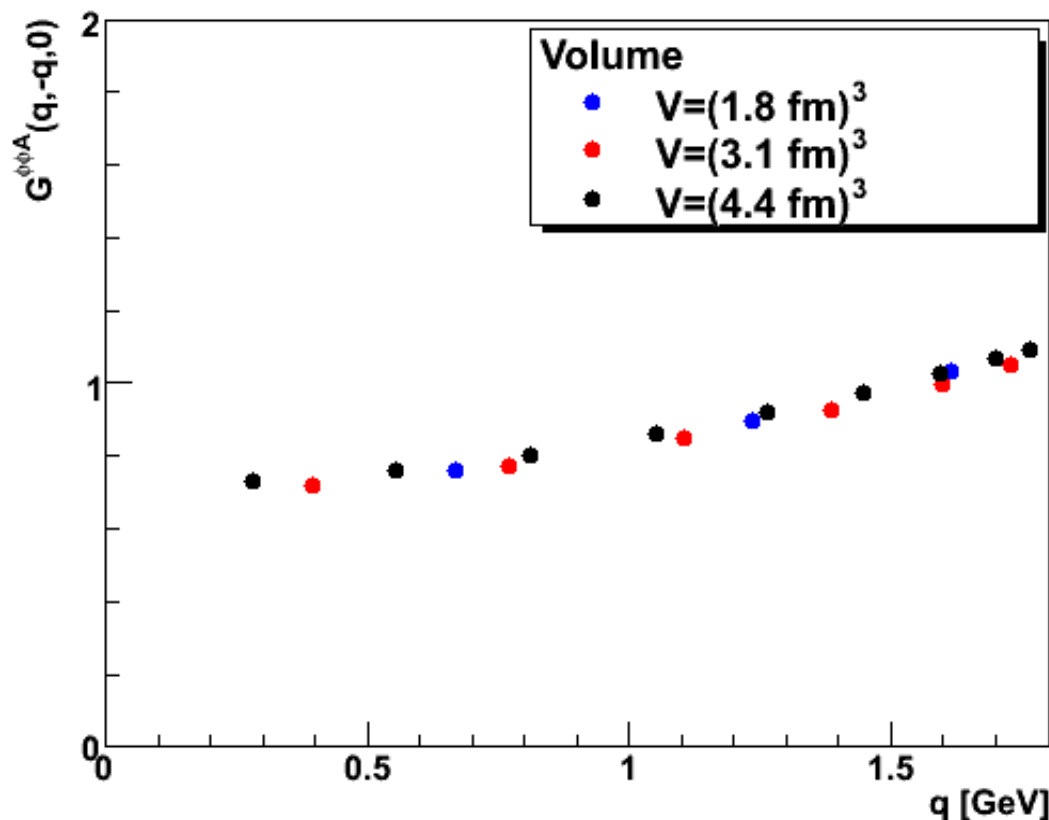
- **Very similar to two and three dimensions**
- **Adjoint and fundamental case renormalize differently**
 - **Increases vs. decreases with cut-off**

Volume dependence mass zero

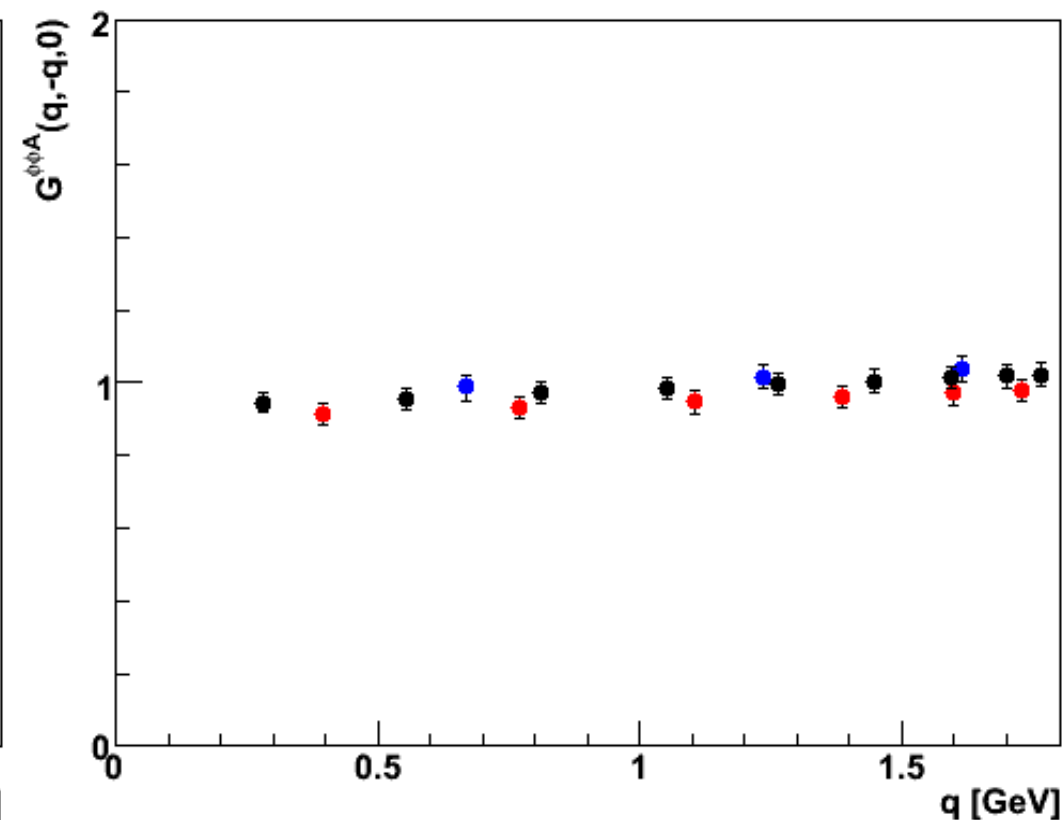
3d, $a=0.22$ fm

[Maas unpublished]

Gluon-2-adjoint-scalar vertex, soft point



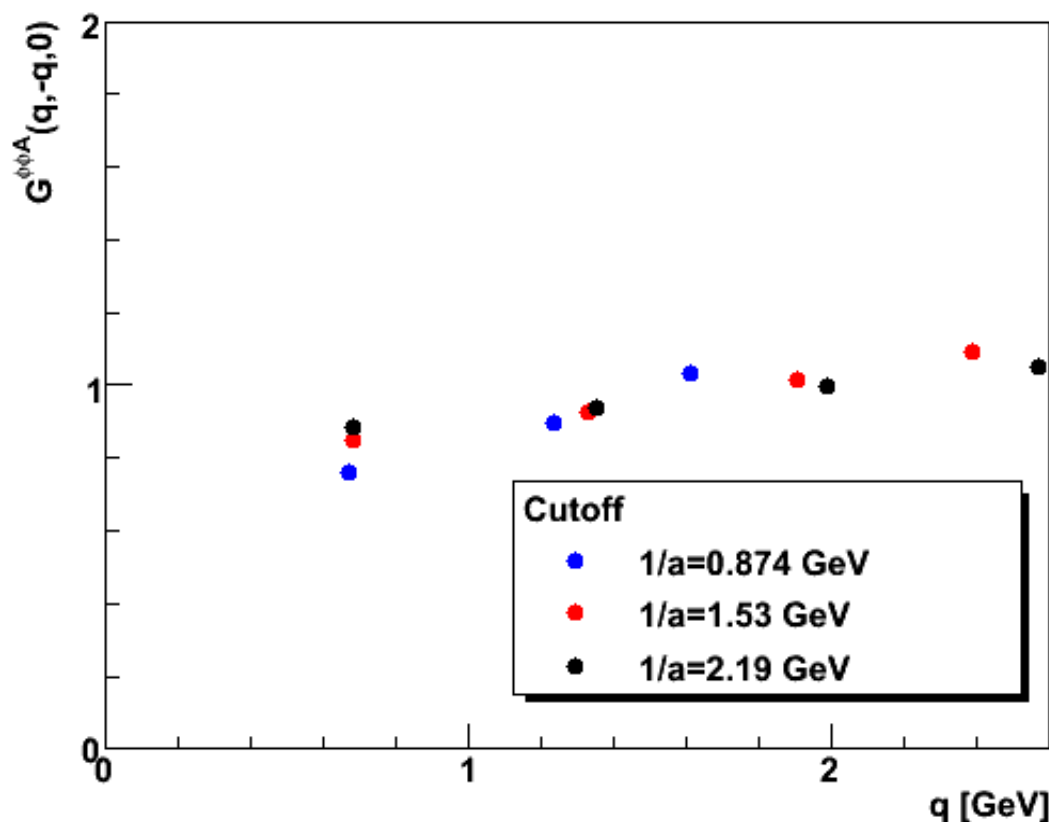
Gluon-2-fundamental-scalar vertex, soft point



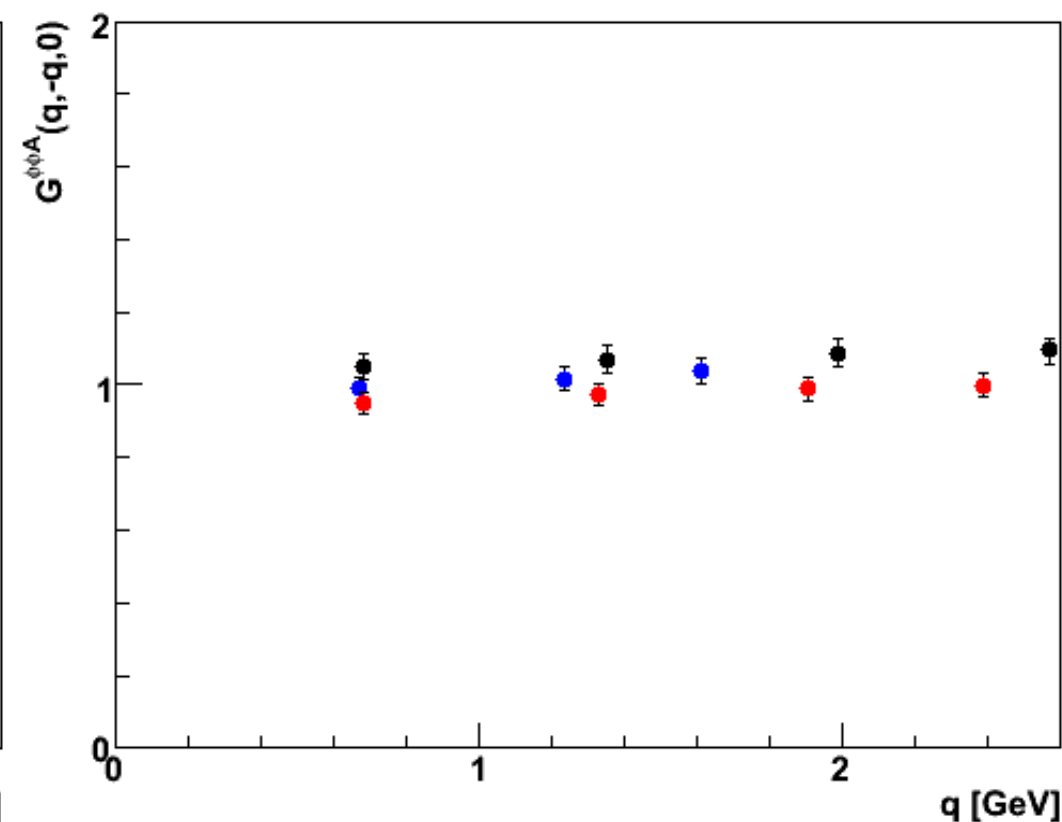
- Adjoint vertex shows almost no effect
- Fundamental vertex shows almost no effect

Cutoff dependence mass zero

Gluon-2-adjoint-scalar vertex, soft point



Gluon-2-fundamental-scalar vertex, soft point



- Reduces adjoint vertex suppression
- Fundamental vertex little affected
- Also some significant effects up to momenta of order $2/a$ for small $1/a$

Quenched summary

- **Adjoint and fundamental start to show different behaviors for both propagators and vertices**

Quenched summary

- **Adjoint and fundamental start to show different behaviors for both propagators and vertices**
- **Volume and discretization effects are both existing and of similar sizes**
- **Requires a careful map of the volume and discretization plane**

Quenched summary

- **Adjoint and fundamental start to show different behaviors for both propagators and vertices**
- **Volume and discretization effects are both existing and of similar sizes**
- **Requires a careful map of the volume and discretization plane**
- **No obvious interpretation of the physics yet**

Quenched summary

- **Adjoint and fundamental start to show different behaviors for both propagators and vertices**
- **Volume and discretization effects are both existing and of similar sizes**
- **Requires a careful map of the volume and discretization plane**
- **No obvious interpretation of the physics yet**
 - **Dynamical mass generation seems to be present**

Dynamical fundamental scalars

- **Scalar matter**

$$L = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \phi^\dagger \left(\frac{1}{2} D_\mu D^\mu + m^2 \right) \phi + \lambda (\phi^\dagger \phi)^2 - \bar{c} \partial^\mu D_\mu c$$

$$D_\mu = \partial_\mu - ie A_\mu^a \tau^a$$

Dynamical fundamental scalars

- **Scalar matter**

$$L = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \phi^+ \left(\frac{1}{2} D_\mu D^\mu + m^2 \right) \phi + \lambda (\phi^+ \phi)^2 - \bar{c} \partial^\mu D_\mu c$$

$$D_\mu = \partial_\mu - ie A_\mu^a \tau^a$$

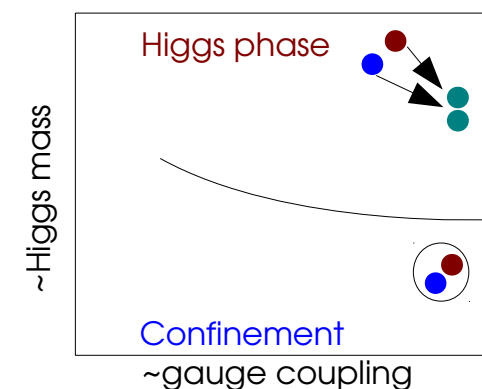
- **Self-interaction not present for quarks**
 - **Dependency not fully explored**
 - **But generically weak at large coupling**
 - **Triviality? Interactions are gauge-dependent!**

Dynamical fundamental scalars

- **Interesting questions:**
 - **Changes compared to the quenched case: String breaking?**

Dynamical fundamental scalars

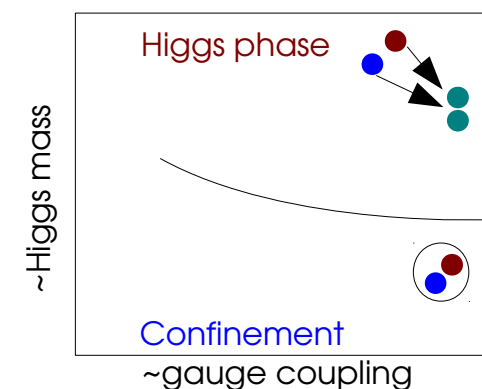
- **Interesting questions:**
 - Changes compared to the quenched case: **String breaking?**
 - **Problem: Higgs mechanism**
 - No (gauge-invariant) difference of confinement and Higgs phase
 - Is this influencing the string breaking compared to QCD?



[Fradkin & Shenker, 1979]

Dynamical fundamental scalars

- **Interesting questions:**
 - Changes compared to the quenched case: **String breaking?**
 - **Problem: Higgs mechanism**
 - No (gauge-invariant) difference of confinement and Higgs phase
 - Is this influencing the string breaking compared to QCD?
- **Propagators in minimal Landau-'t Hooft gauge**



[Fradkin & Shenker, 1979]

Gauge bosons

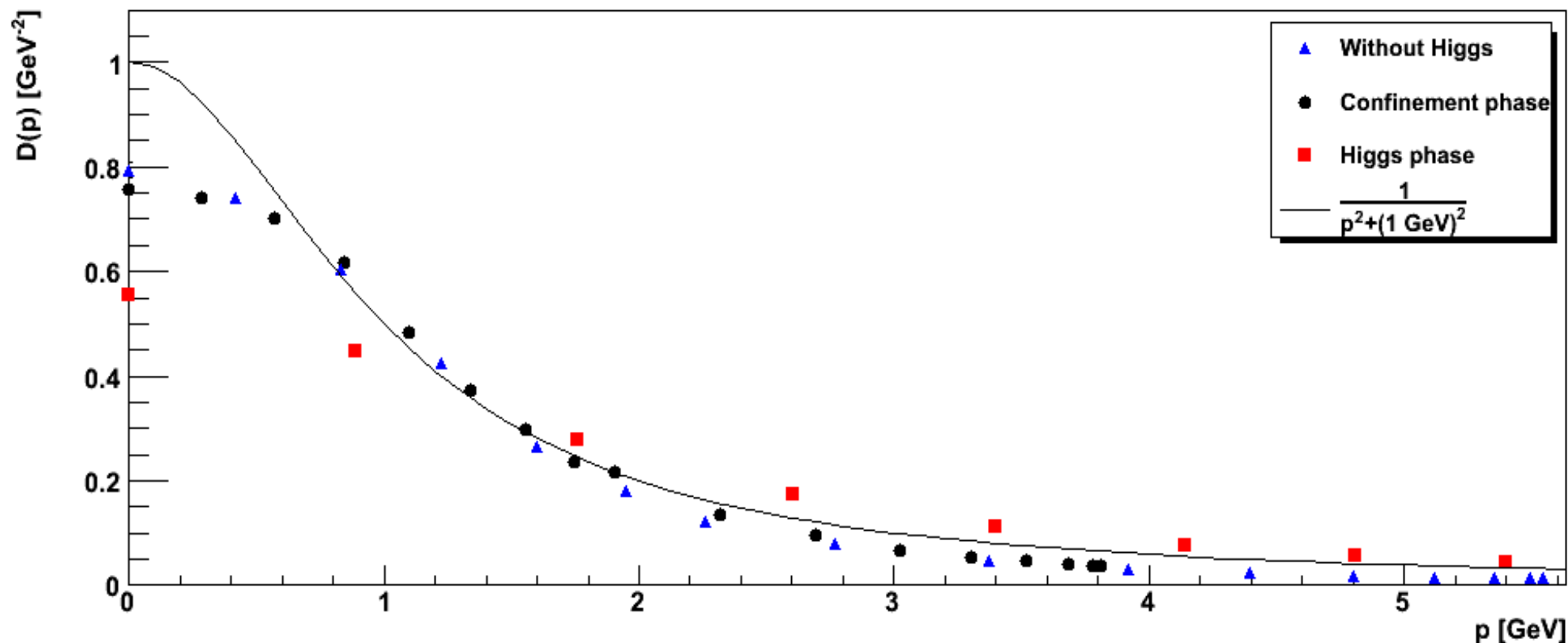
4d, unquenched: 24^4 beta=2.0, kappa=0.25, lambda=0.5

4d, Higgs, 24^4 beta=2.3, kappa=0.32, lambda=1.0

4d, quenched: 24^4 beta=2.2

[Maas 2010]

Gauge boson propagator



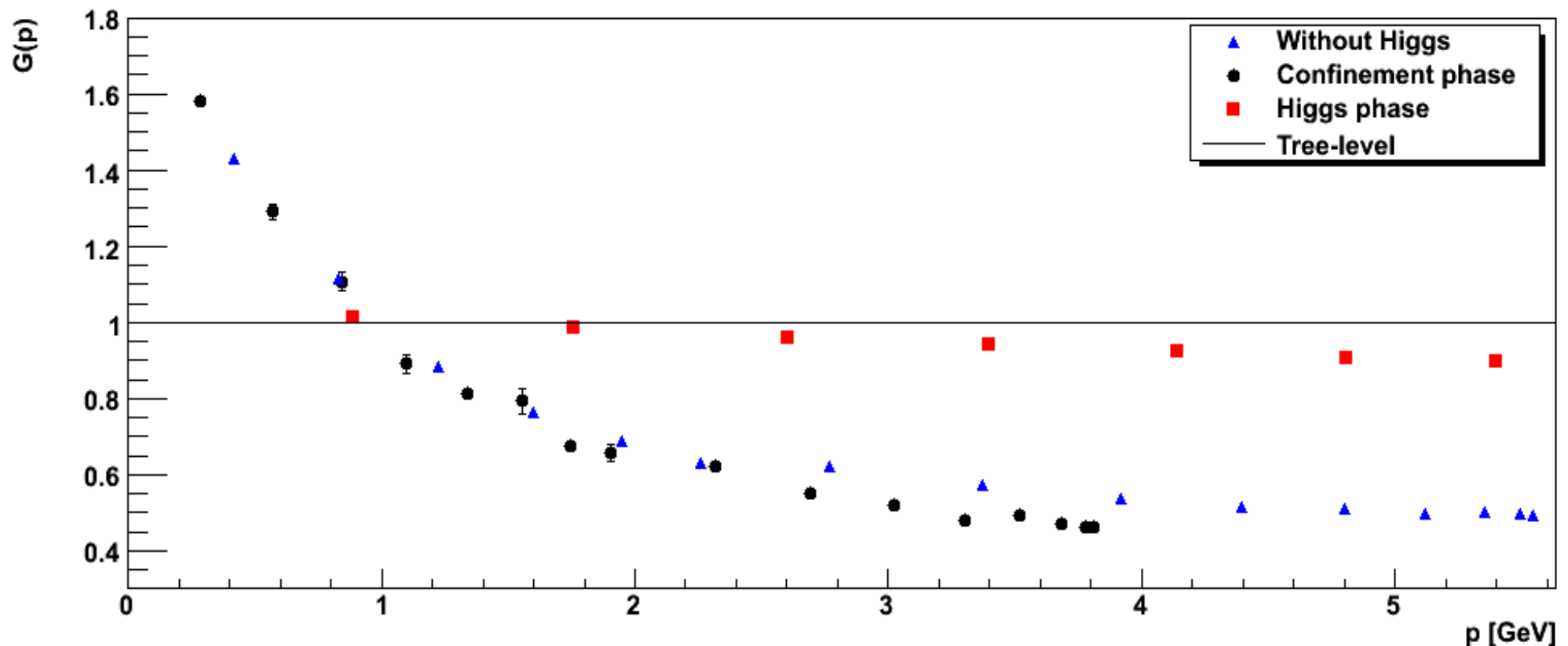
- **Little qualitative difference – impact of matter and 'phase' small**
- **As in QCD** [Fischer, Alkofer PRD03, Kamleh et al. PRD07]

Ghosts

4d, unquenched: 24^4 beta=2.0, kappa=0.25, lambda=0.5
 4d, Higgs, 24^4 beta=2.3, kappa=0.32, lambda=1.0
 4d, quenched: 24^4 beta=2.2

[Maas 2010]

Ghost dressing function



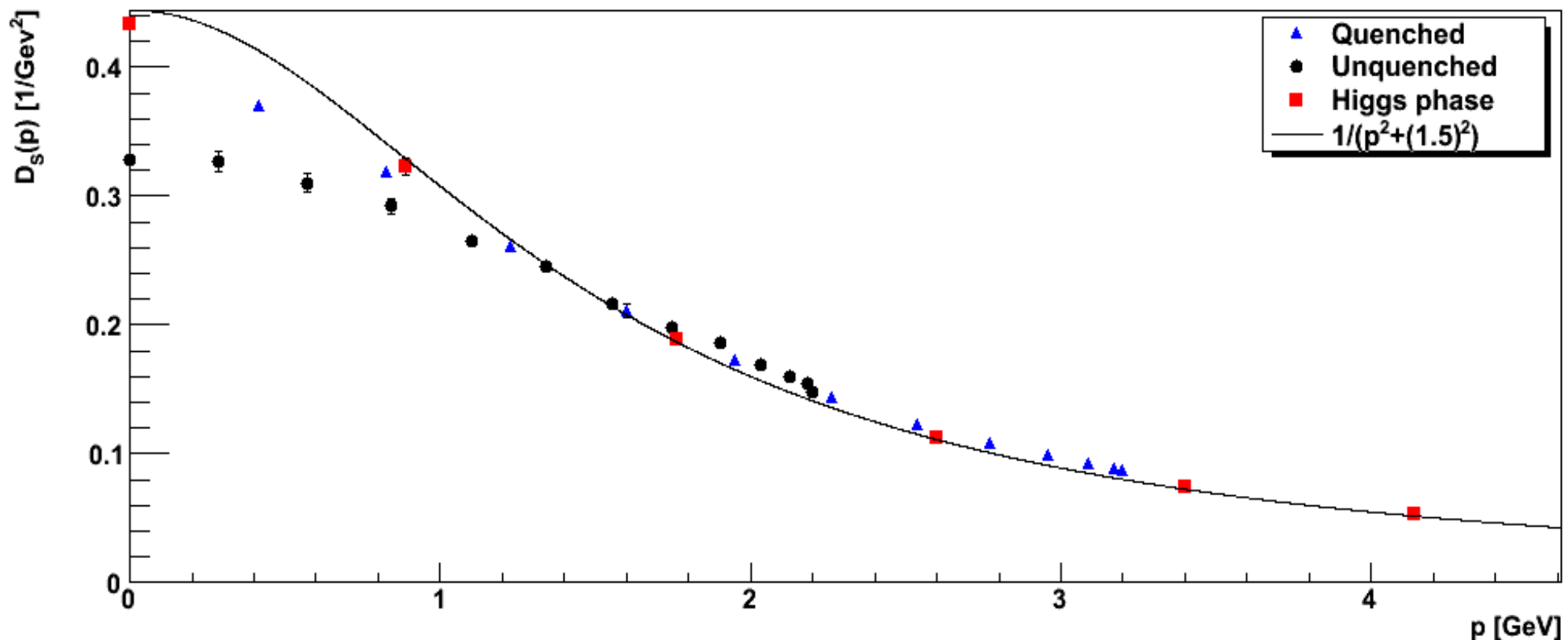
- **Significant impact of 'phase', but not of matter**
- **Much more photon-like in the Higgs 'phase'**
 - **As in Coulomb gauge** [Greensite, Olejnik, Zwanziger 2004]

Scalar

4d, unquenched: 24^4 beta=2.0, kappa=0.25, lambda=0.5
 4d, Higgs, 24^4 beta=2.3, kappa=0.32, lambda=1.0
 4d, quenched: 24^4 beta=2.2

[Maas 2010]

Scalar propagator



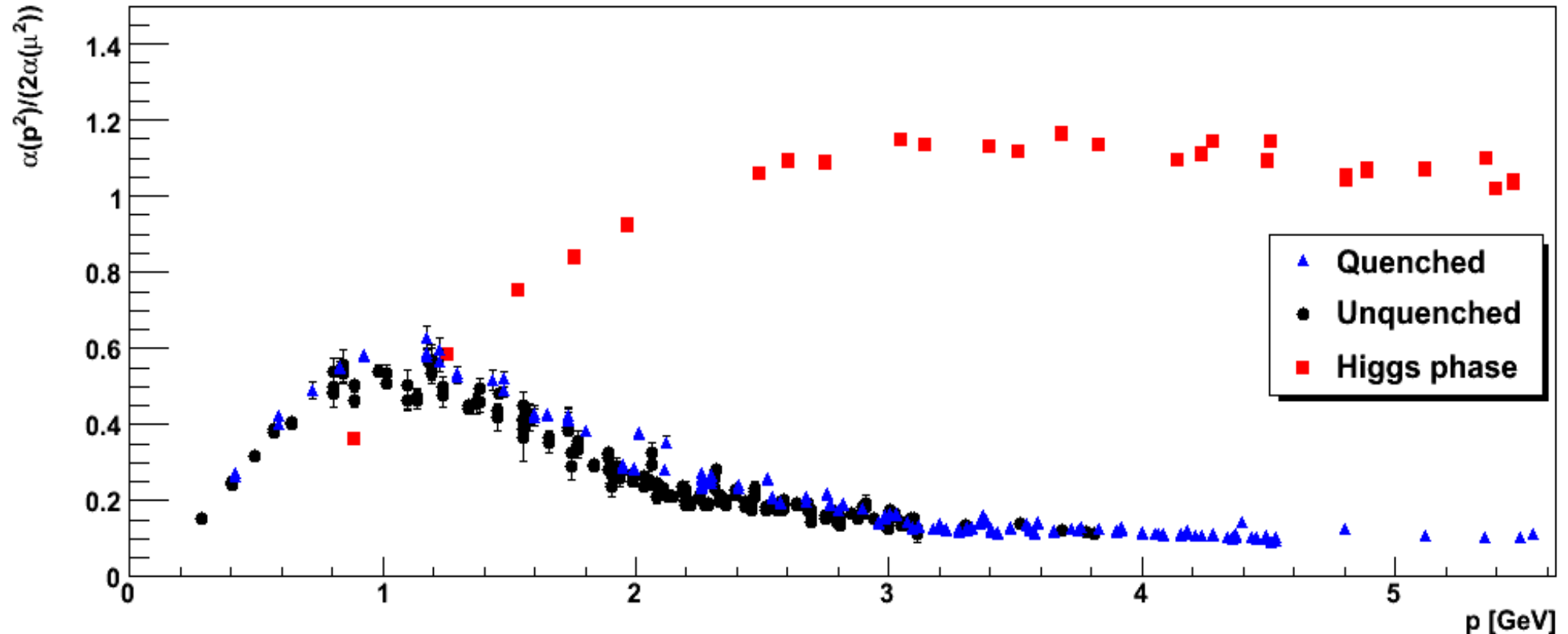
- Close to tree-level with renormalized mass
- Little difference between the 'phases'
- Again dynamical mass generation

Running coupling

4d, unquenched: 24^4 beta=2.0, kappa=0.25, lambda=0.5
 4d, Higgs, 24^4 beta=2.3, kappa=0.32, lambda=1.0
 4d, quenched: 24^4 beta=2.2

[Maas 2010]

Running coupling



- No qualitative difference seen
- Screening leads to suppression of interactions at small momenta

Summary

- **Scalar particles are a laboratory to investigate strong interactions physics**
 - **Simple tensor structures**
 - **String/confinement physics**
 - **Representation dependence**
 - **No complications due to chiral symmetry**

Summary

- **Scalar particles are a laboratory to investigate strong interactions physics**
 - **Simple tensor structures**
 - **String/confinement physics**
 - **Representation dependence**
 - **No complications due to chiral symmetry**
- **(Quenched) adjoint and fundamental scalars appear differently**
 - **Sensitive to volume and discretization effects**
 - **Interpretation in terms of a string?**

Summary

- **Scalar particles are a laboratory to investigate strong interactions physics**
 - **Simple tensor structures**
 - **String/confinement physics**
 - **Representation dependence**
 - **No complications due to chiral symmetry**
- **(Quenched) adjoint and fundamental scalars appear differently**
 - **Sensitive to volume and discretization effects**
 - **Interpretation in terms of a string?**
- **Unquenching has no qualitative impact**
 - **Higgs 'phase' may be different**

Summary

- **Scalar particles are a laboratory to investigate strong interactions physics**
 - Simple tensor structures
 - String/confinement physics
 - Representation dependence
 - No complications due to chiral symmetry
- **(Quenched) adjoint and fundamental scalars appear differently**
 - Sensitive to volume and discretization effects
 - Interpretation in terms of a string?
- **Unquenching has no qualitative impact**
 - Higgs 'phase' may be different

Modified coupling

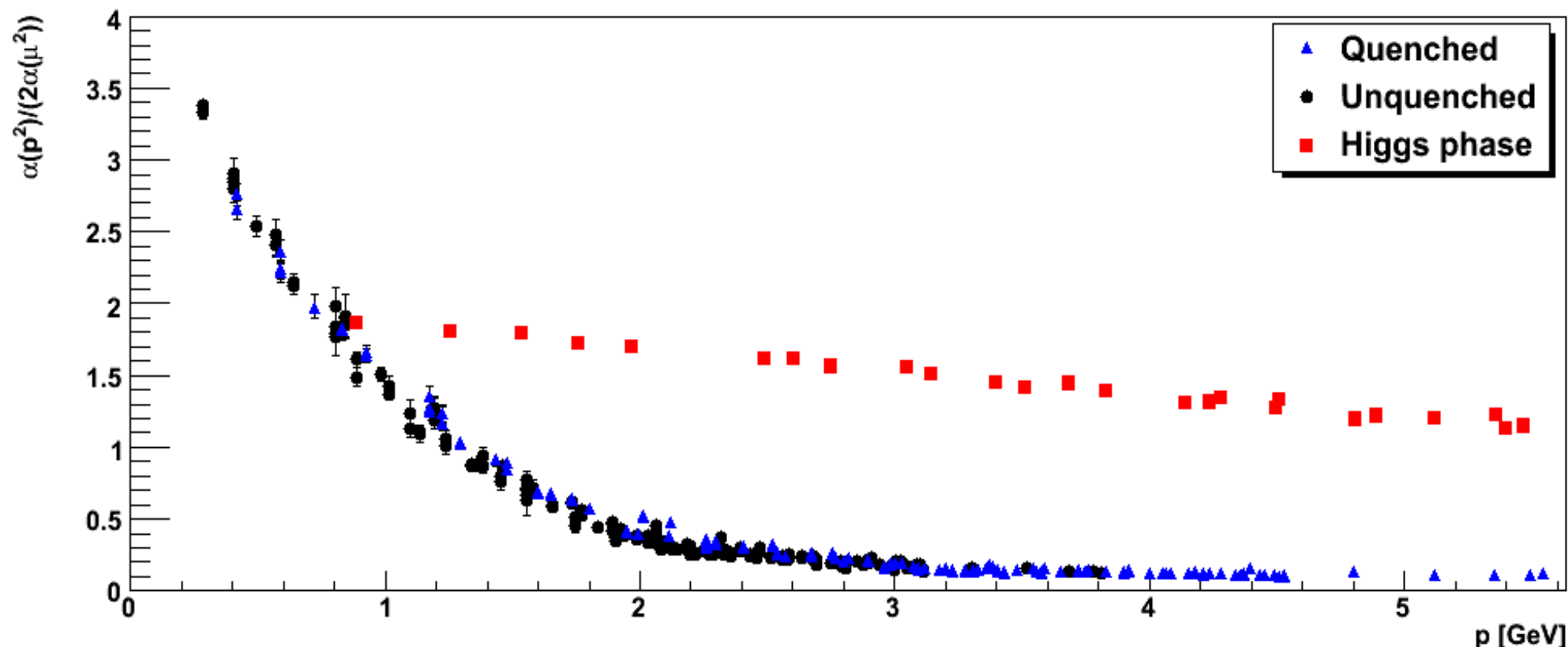
4d, unquenched: 24^4 beta=2.0, kappa=0.25, lambda=0.5

4d, Higgs, 24^4 beta=2.3, kappa=0.32, lambda=1.0

4d, quenched: 24^4 beta=2.2

[Maas 2010]

Modified running coupling



- Infrared parameter is the screening mass of the gluon
- No qualitative difference – both finite